

# Intro to Inferential Statistics with R

Workshop 5

Course: VSK1004 Applied Researcher



# Workshop structure (draft)

MONDAY	WEDNESDAY	TODAY
Intro to Statistic Inference	More about inferential stats	Linear & Logistic Regression
<ol style="list-style-type: none"><li>1. Descriptive vs Inferential statistics</li><li>2. Population, sample and sampling distribution</li><li>3. Null Hypothesis testing</li><li>4. Correlation and interpretation</li></ol>	<ol style="list-style-type: none"><li>1. Choosing a statistical test</li><li>2. t-test family</li><li>3. chi-squared</li><li>4. correlation</li><li>5. Chi-squared distribution</li></ol>	<ol style="list-style-type: none"><li>1. Linear Regression</li><li>2. Multiple Linear Regression</li><li>3. Model Assumption</li><li>4. Logistic Regression</li></ol>



# Our goal in the next 40 min

In this session, we will cover some of the **basic statistical models and its properties** such as:

1. Simple Linear Regression
2. Multiple Linear Regression
3. Linear Model Assumptions
4. Logistic Regression



# Simple Linear Regression



# The mathematical equation

Simple  
Linear  
Regression

$$y = b_0 + b_1 * x_1$$



# The mathematical equation

Simple  
Linear  
Regression

$$y = b_0 + b_1 * x_1$$

Dependent variable (DV)



# The mathematical equation

Simple  
Linear  
Regression

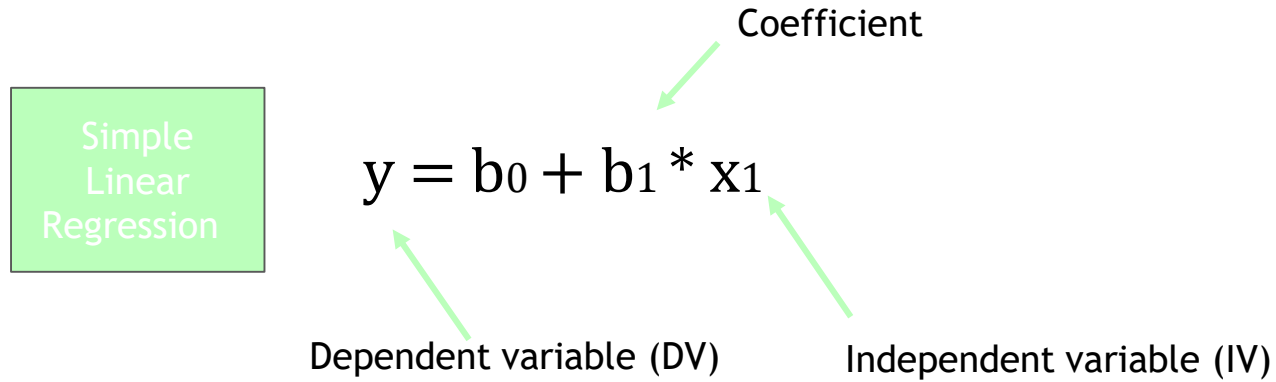
$$y = b_0 + b_1 * x_1$$

Dependent variable (DV)

Independent variable (IV)



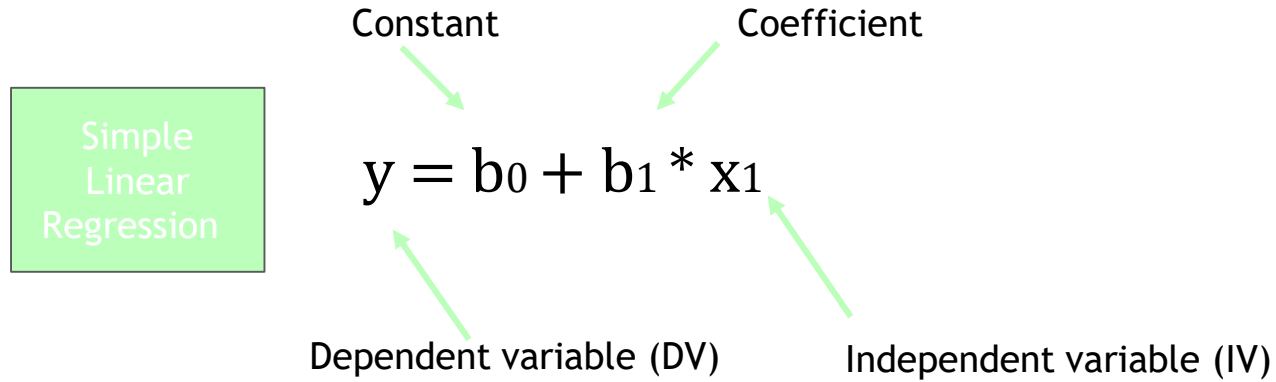
# The mathematical equation







# The mathematical equation



# Look at the simple Linear regression

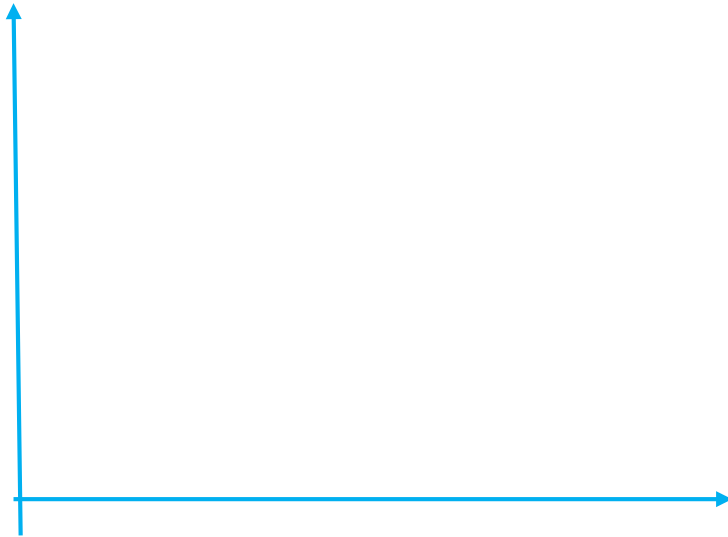
## Simple Linear Regression:



# Representation in a graph: x and y axis

## Simple Linear Regression:

Salary (Euro)

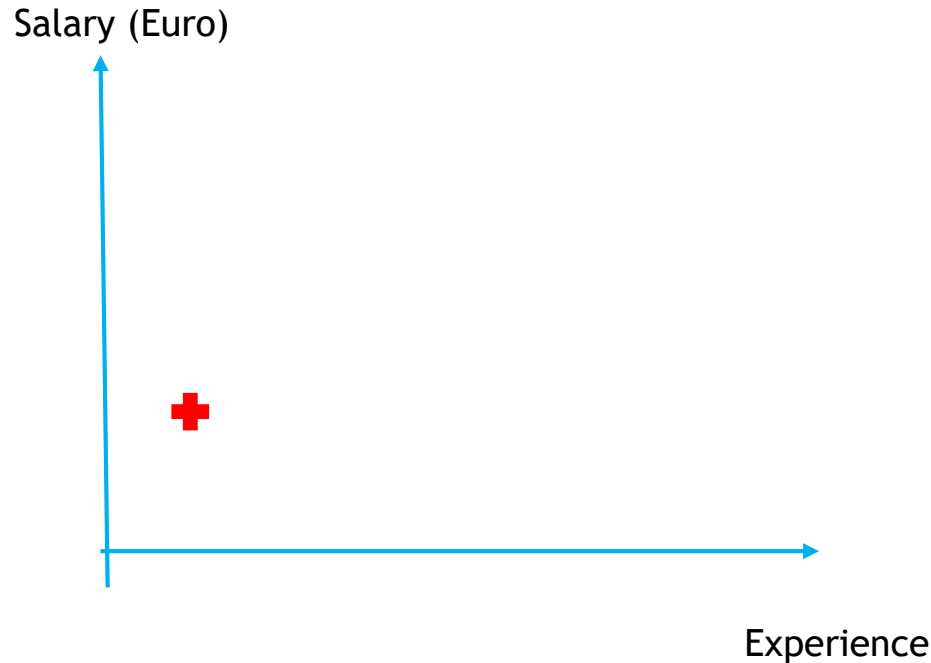


Experience



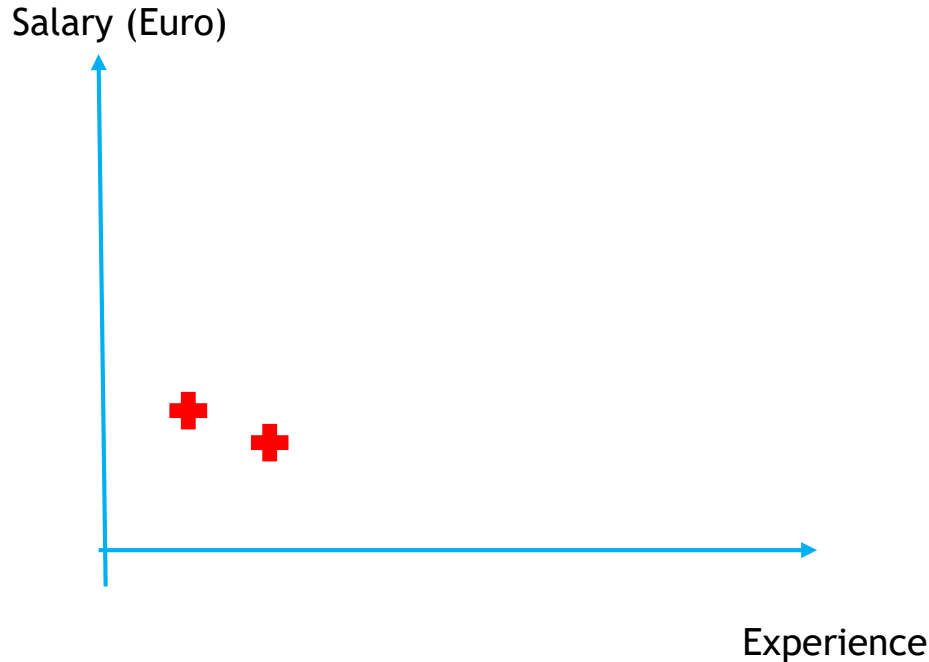
# Representation in a graph: dots as observed data

## Simple Linear Regression:



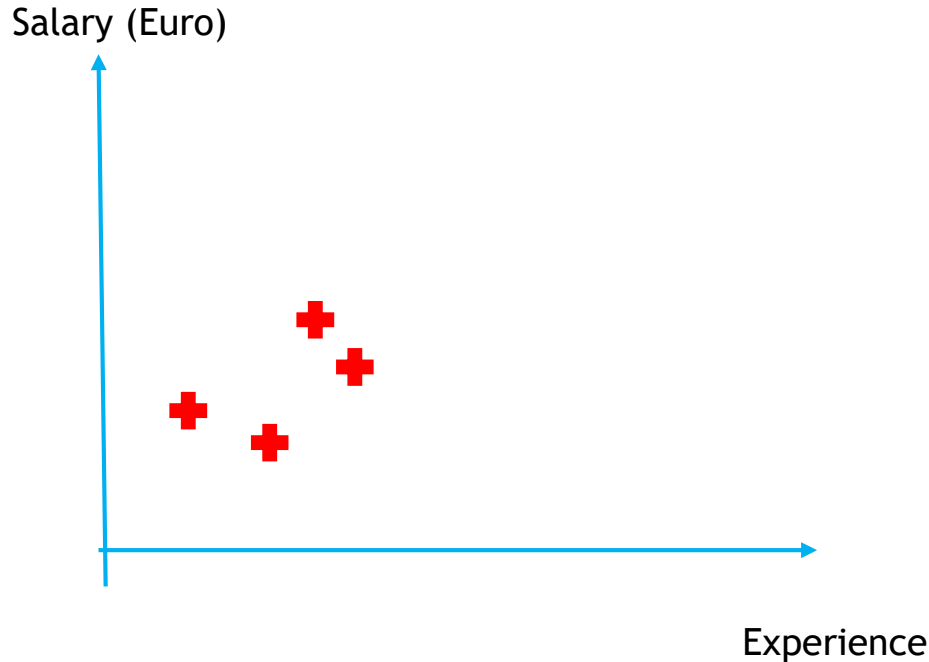
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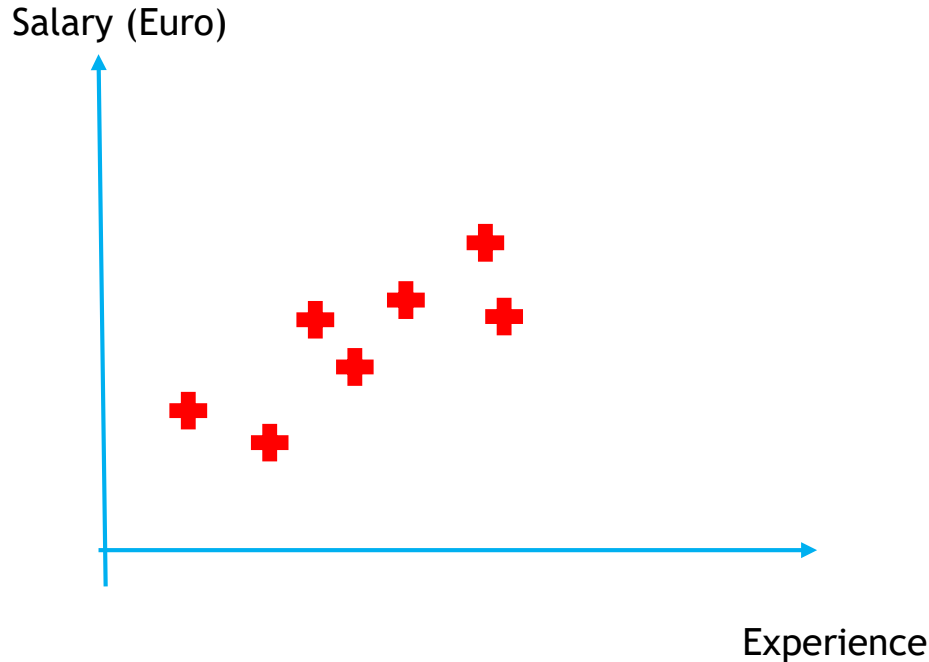
# Representation in a graph: dots as observed data

## Simple Linear Regression:



# Representation in a graph: dots as observed data

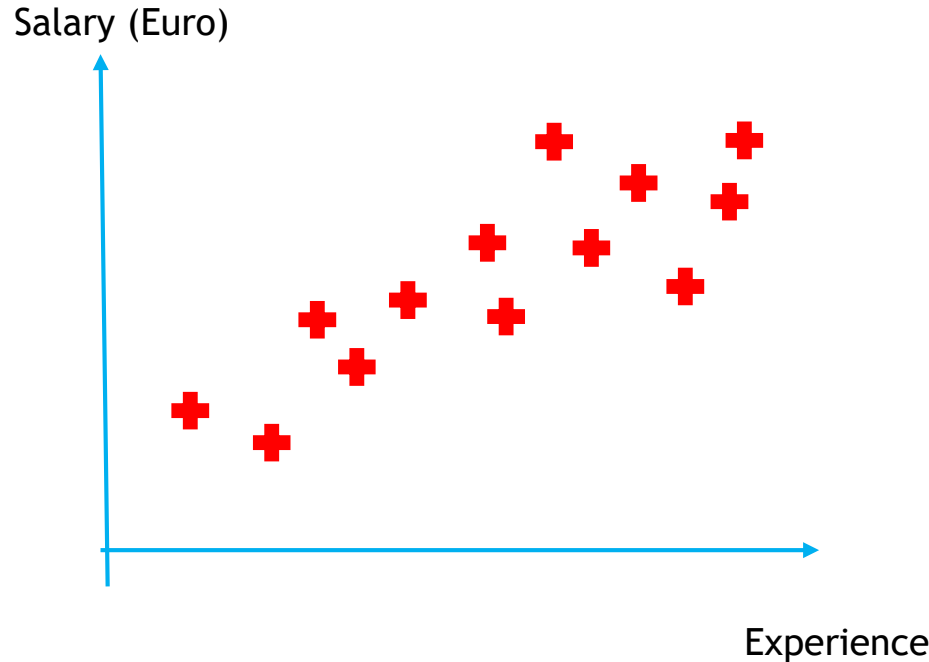
## Simple Linear Regression:





# how salary is distributed among people

## Simple Linear Regression:

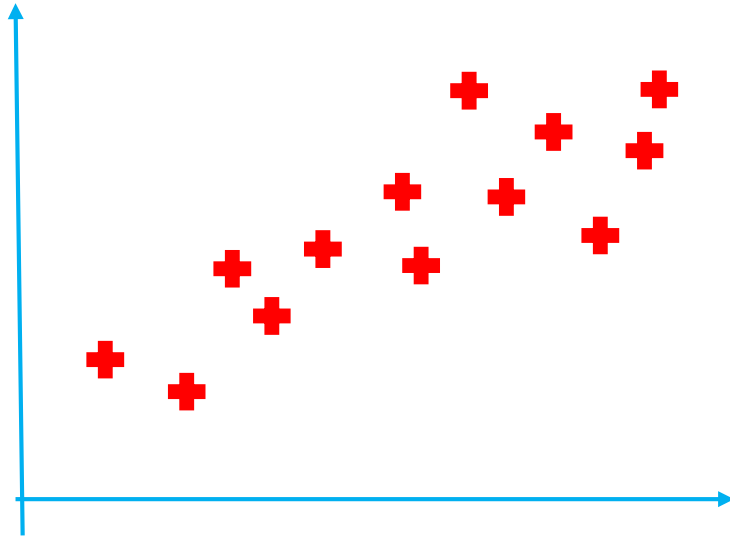




# Representation in a graph: observed data

## Simple Linear Regression:

Salary (Euro)



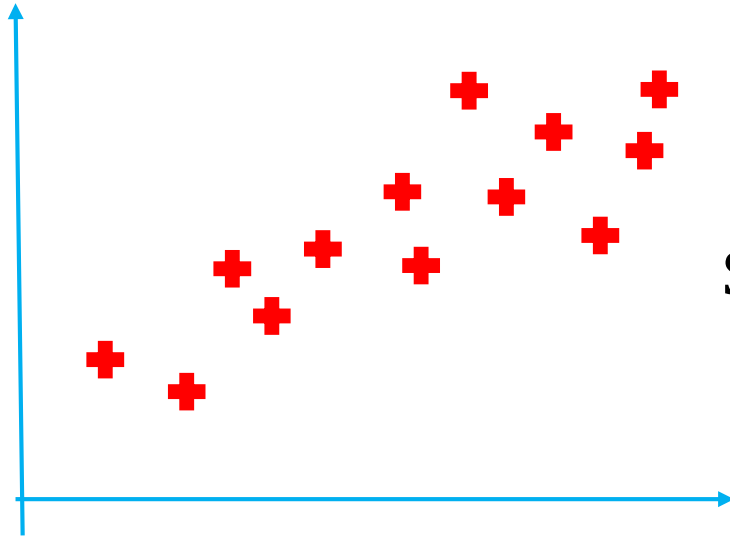
$$y = b_0 + b_1 * x_1$$



# Representation in a graph with the equation

## Simple Linear Regression:

Salary (Euro)



$$y = b_0 + b_1 * x_1$$

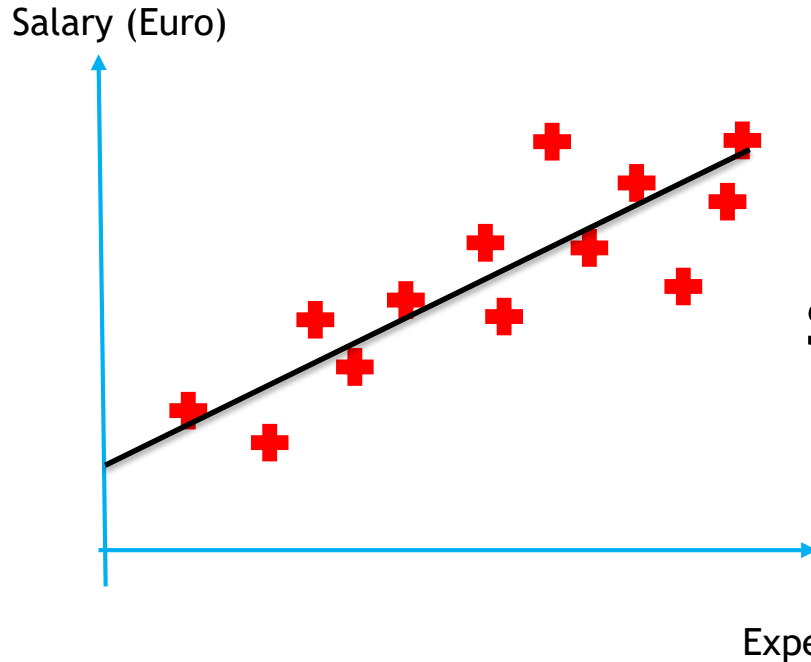


$$\text{Salary} = b_0 + b_1 * \text{Experience}$$



# Add best fitting line for linear regression

## Simple Linear Regression:



$$y = b_0 + b_1 * x_1$$



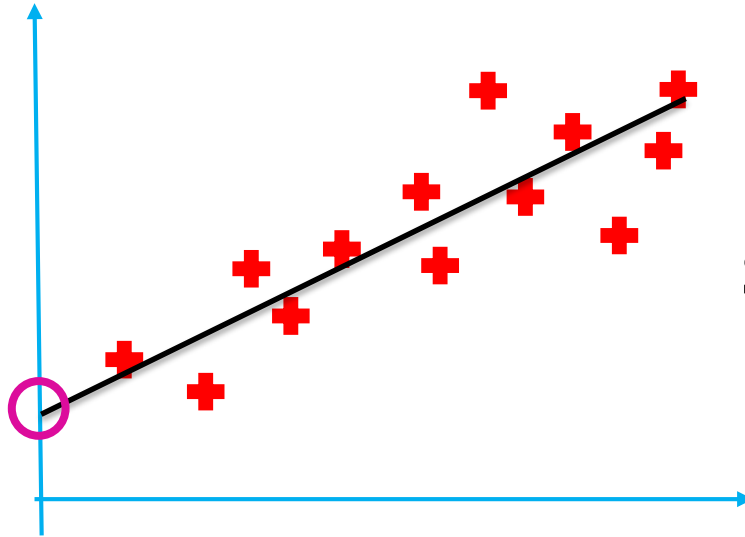
$$\text{Salary} = b_0 + b_1 * \text{Experience}$$



# Identify parameters in the graphs: Constant

## Simple Linear Regression:

Salary (Euro)



$$y = b_0 + b_1 * x_1$$

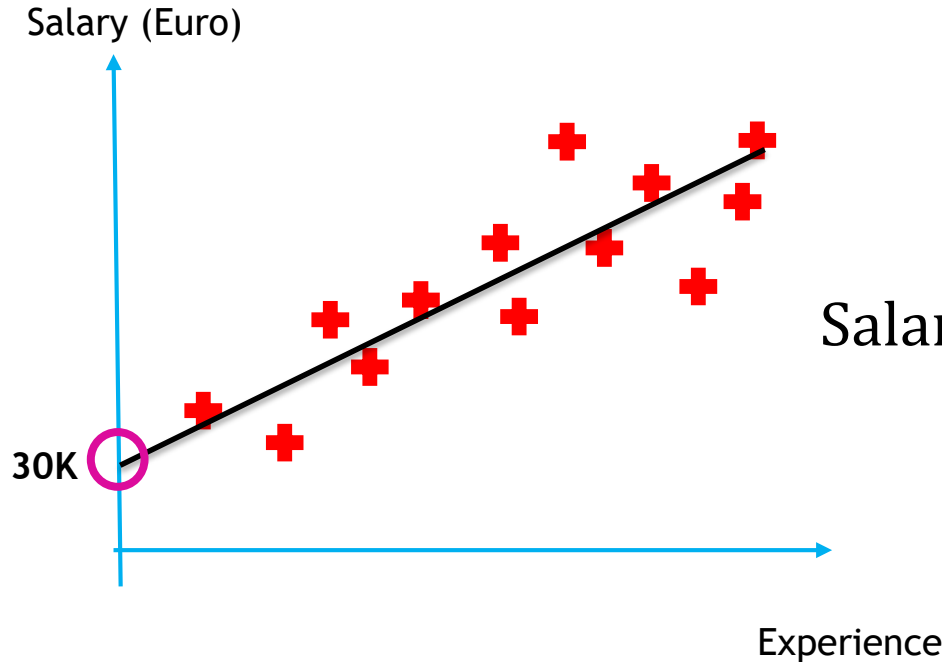


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# Identify parameters in the graphs: Constant

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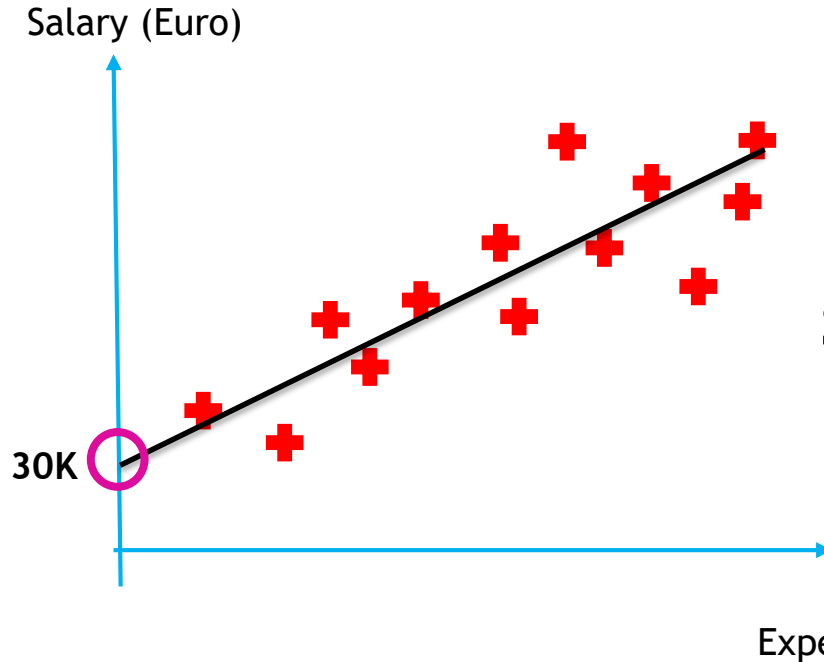


$$\text{Salary} = b_0 + b_1 * \text{Experience}$$



# Identify parameters in the graphs: Slope

## Simple Linear Regression:



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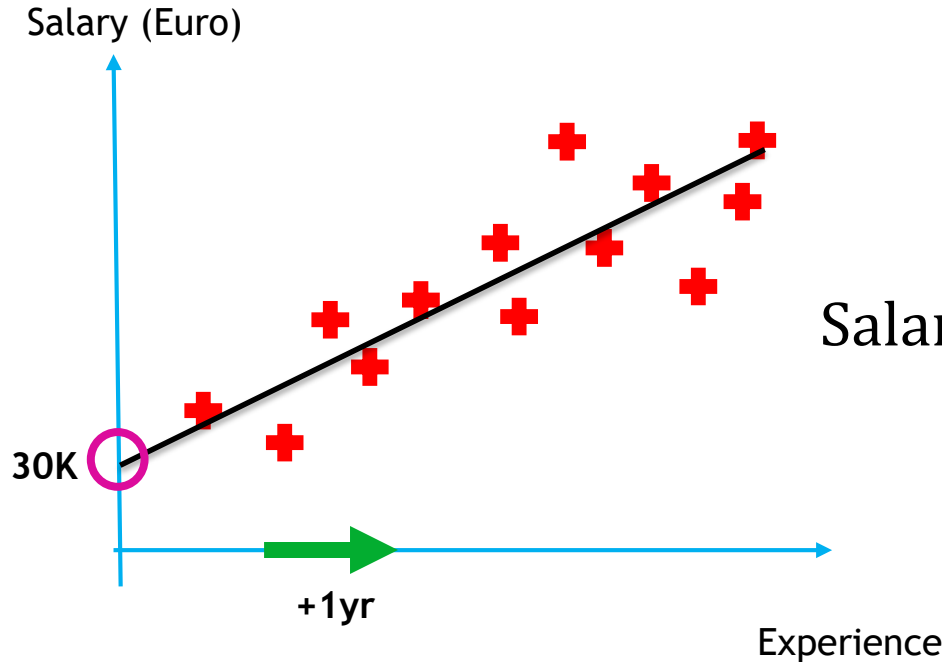


$$\text{Salary} = b_0 + b_1 * \text{Experience}$$



# Identify parameters in the graphs: Slope

## Simple Linear Regression:



$$y = b_0 + b_1 * x_1$$

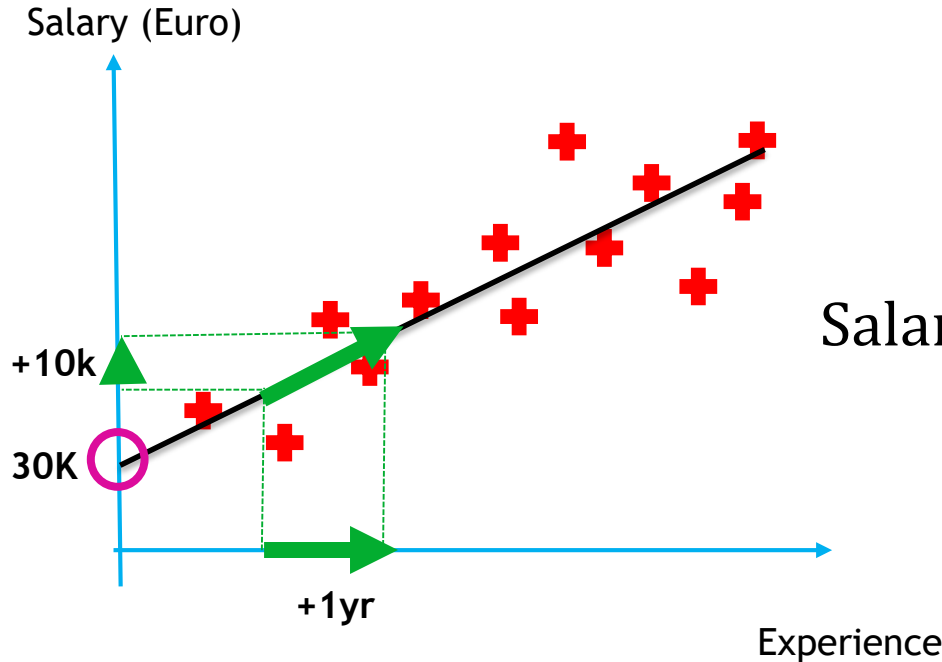


$$\text{Salary} = b_0 + b_1 * \text{Experience}$$



# Identify parameters in the graphs: Slope

## Simple Linear Regression:



$$y = b_0 + b_1 * x_1$$



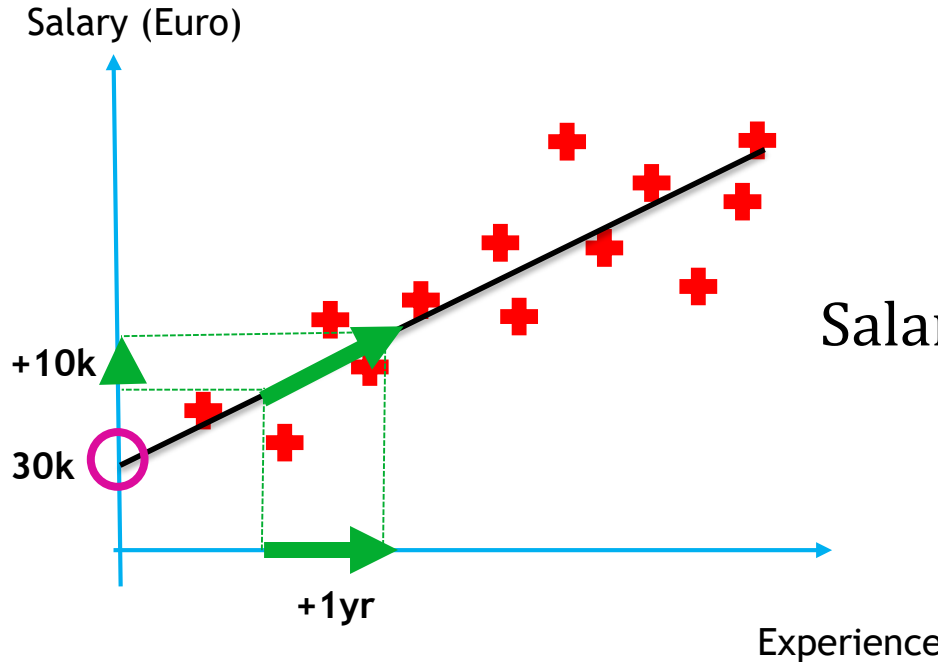
$$\text{Salary} = b_0 + b_1 * \text{Experience}$$





# All linear parameters in the best fitted line

## Simple Linear Regression:



$$y = b_0 + b_1 * x_1$$

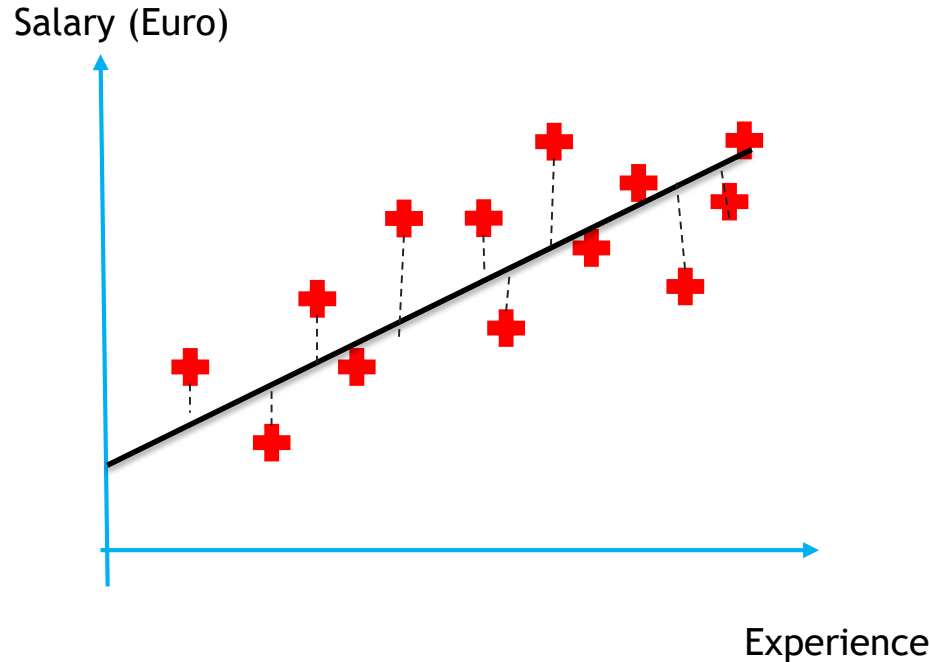


$$\text{Salary} = b_0 + b_1 * \text{Experience}$$



# How linear regression find best fitting line?

## Simple Linear Regression:

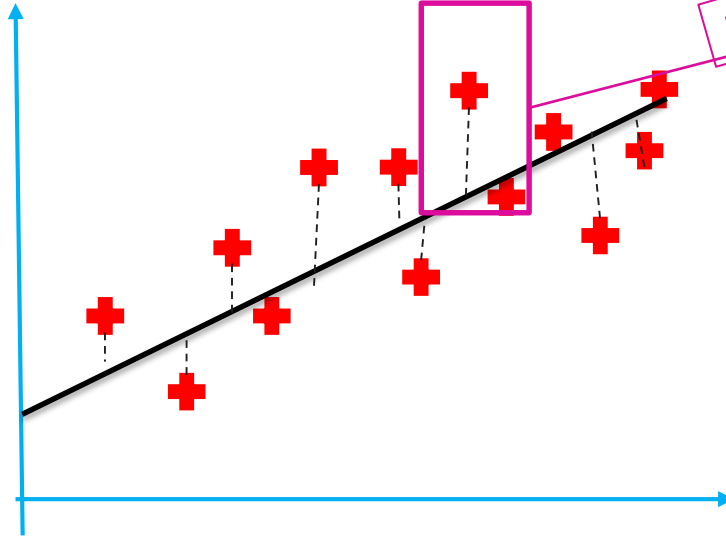




# How linear regression find best fitting line

## Simple Linear Regression:

Salary (Euro)



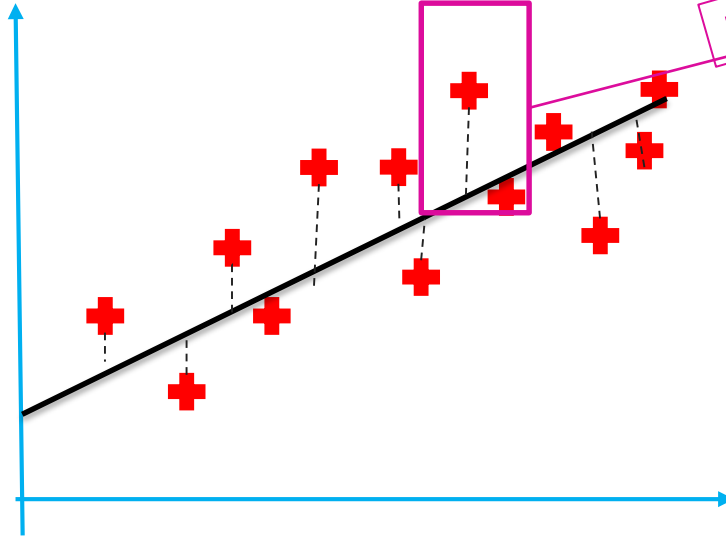
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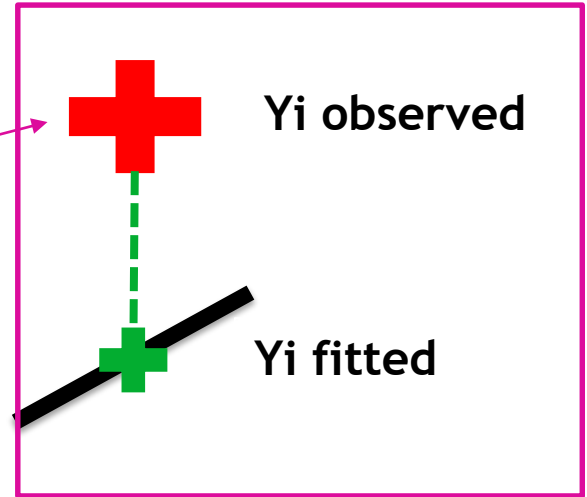
# How linear regression find best fitting line

## Simple Linear Regression:

Salary (Euro)



Example

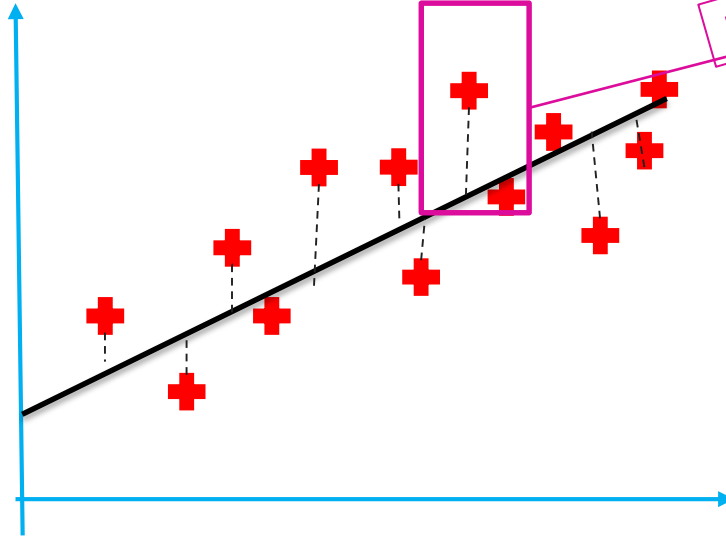




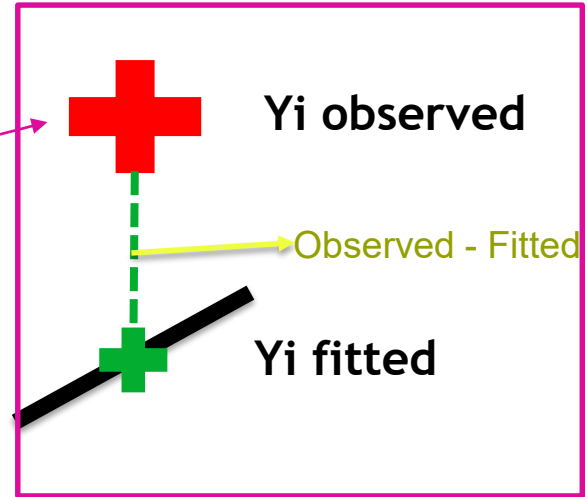
# How linear regression find best fitting line

## Simple Linear Regression:

Salary (Euro)



Example

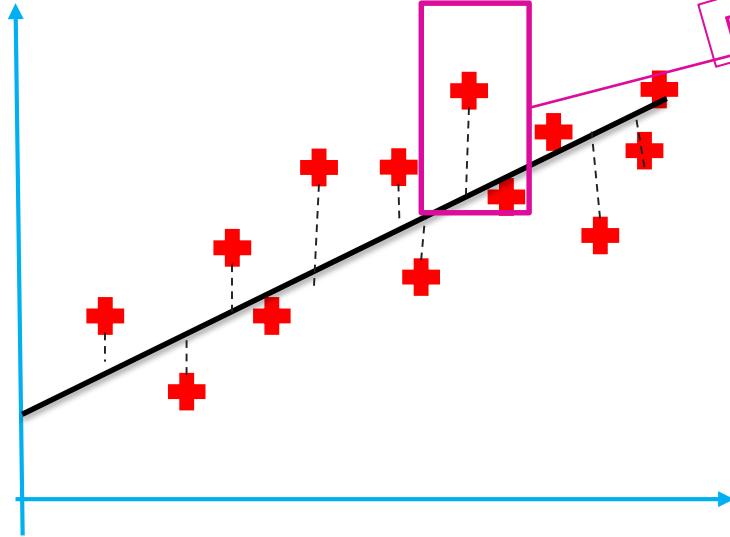




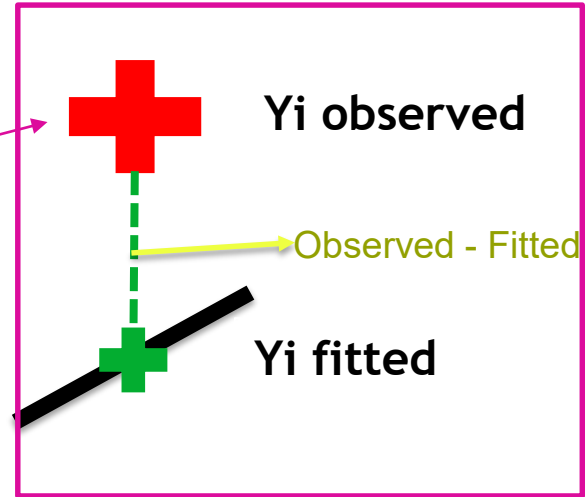
# How linear regression find best fitting line

## Simple Linear Regression:

Salary (Euro)



Example



$$\text{SUM } (Y_i \text{ observed} - Y_i \text{ fitted})^2$$

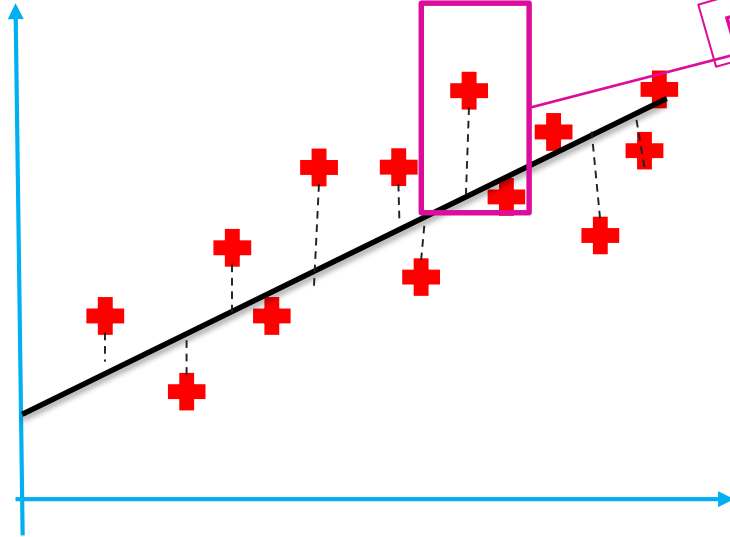
Experience



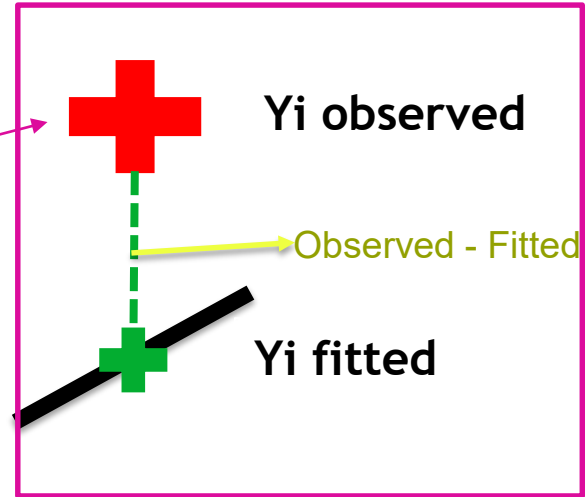
# How linear regression find best fitting line

## Simple Linear Regression:

Salary (Euro)



Example



$SUM (Y_i \text{ observed} - Y_i \text{ fitted})^2 \rightarrow \text{min}$

Experience

Linear Regression looks for min sum of squares to find the line which has the smallest sum squares possible, and its called, the best fitting line





# Multiple Linear Regression



# Same thing but many variables into the model

Simple  
Linear  
Regression

$$y = b_0 + b_1 * x_1$$

Multiple  
Linear  
Regression

$$y = b_0 + b_1 * x_1 + b_2 * x_2 + \dots + b_n * X_n$$


# Same thing but many variables into the model

Simple  
Linear  
Regression

$$y = b_0 + b_1 * x_1$$

Multiple  
Linear  
Regression

Dependent variable (DV)


$$y = b_0 + b_1 * x_1 + b_2 * x_2 + \dots + b_n * X_n$$



# Same thing but many variables into the model

Simple  
Linear  
Regression

$$y = b_0 + b_1 * x_1$$

Multiple  
Linear  
Regression

Dependent variable (DV)

Independent variable (IVs)

$$y = b_0 + b_1 * x_1 + b_2 * x_2 + \dots + b_n * X_n$$

# Regressions

Simple  
Linear  
Regression

$$y = b_0 + b_1 * x_1$$

Multiple  
Linear  
Regression

Dependent variable (DV)      Independent variable (IVs)

$$y = b_0 + b_1 * x_1 + b_2 * x_2 \dots + b_n * X_n$$

Constant      Coefficients

The diagram shows the equation  $y = b_0 + b_1 * x_1 + b_2 * x_2 \dots + b_n * X_n$ . Green arrows point from labels to parts of the equation: 'Dependent variable (DV)' points to 'y'; 'Independent variable (IVs)' points to 'x1', 'x2', and 'Xn'; 'Constant' points to 'b0'; and 'Coefficients' points to 'b1', 'b2', and 'bn'.



# Model Assumptions



# A Caveat: Assumptions of Linear Regression

1. Linearity
2. Homoscedasticity
3. Multivariate Normality
4. Independence of errors
5. Lack of multicollinearity



# Logistic Regression



# What we know

## Linear Regression:

# What we know

## Linear Regression:

- Simple

$$y = b_0 + b_1 * x$$

# What we know

## Linear Regression:

### - Simple

$$y = b_0 + b_1 * x$$

### - Multiple:

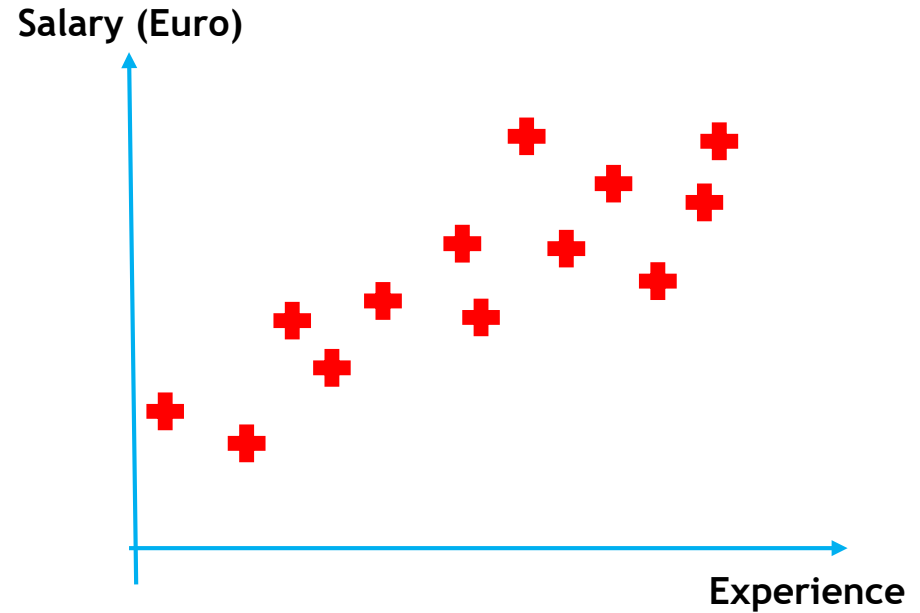
$$y = b_0 + b_1 * x_1 + \dots + b_n * X_n$$

# What we know

**We know this:**

# What we know

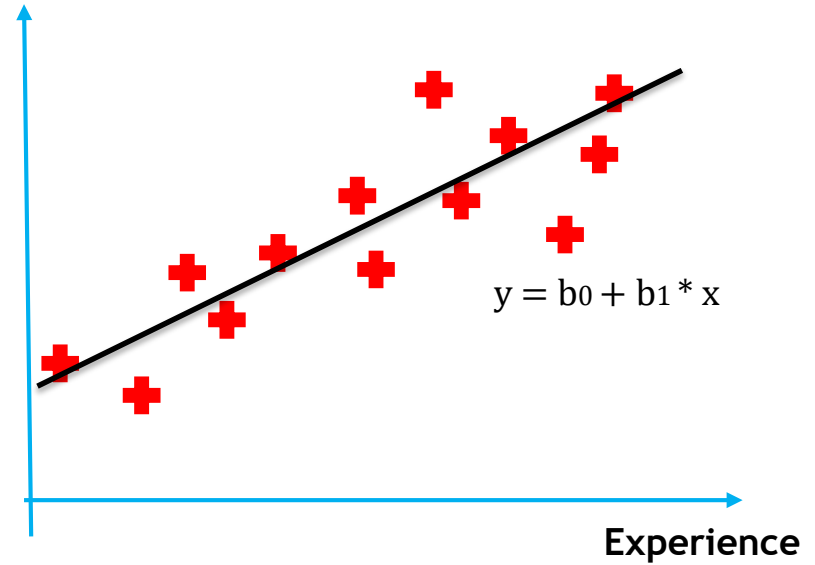
We know this:



# What we know

## We know this:

Salary (Euro)

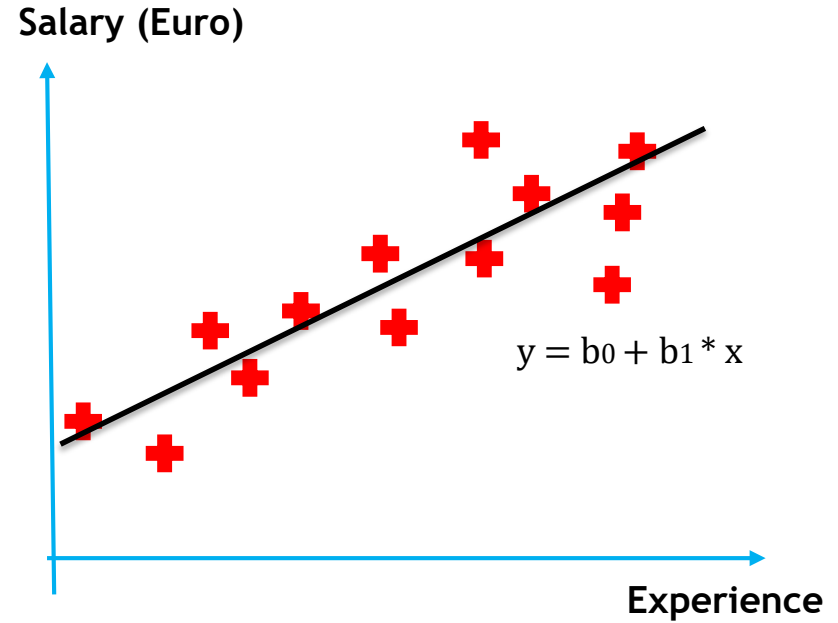




# What is new: Logistic regression

This is new:

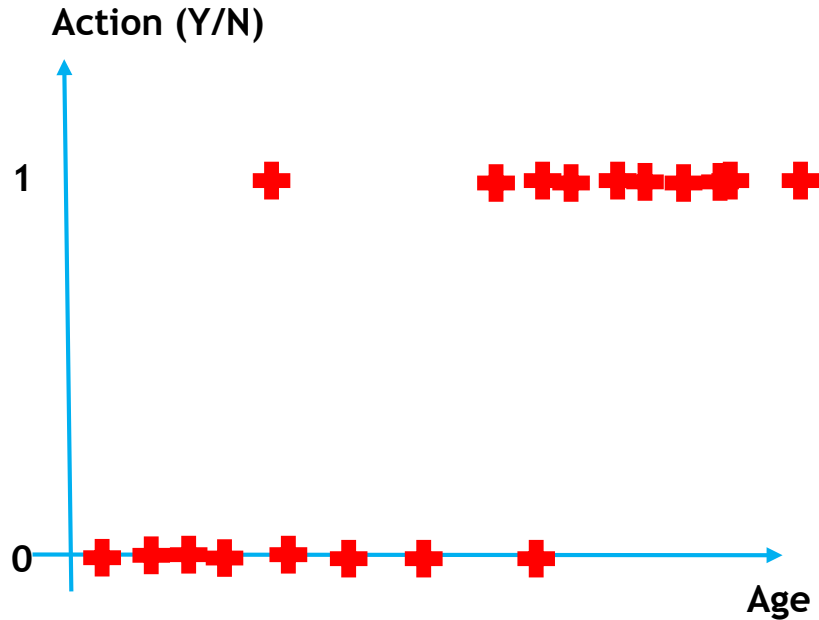
We know this:



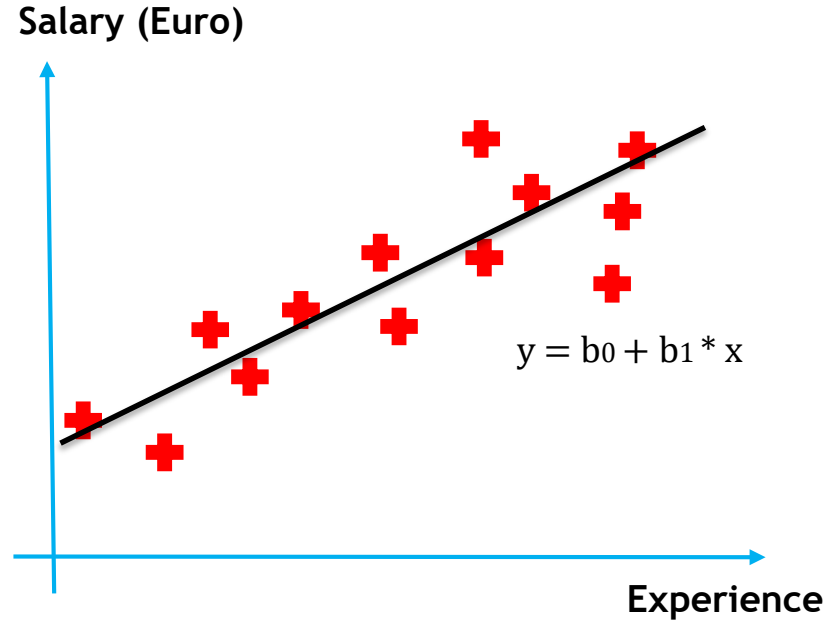


# Logistic regression

This is new:



We know this:

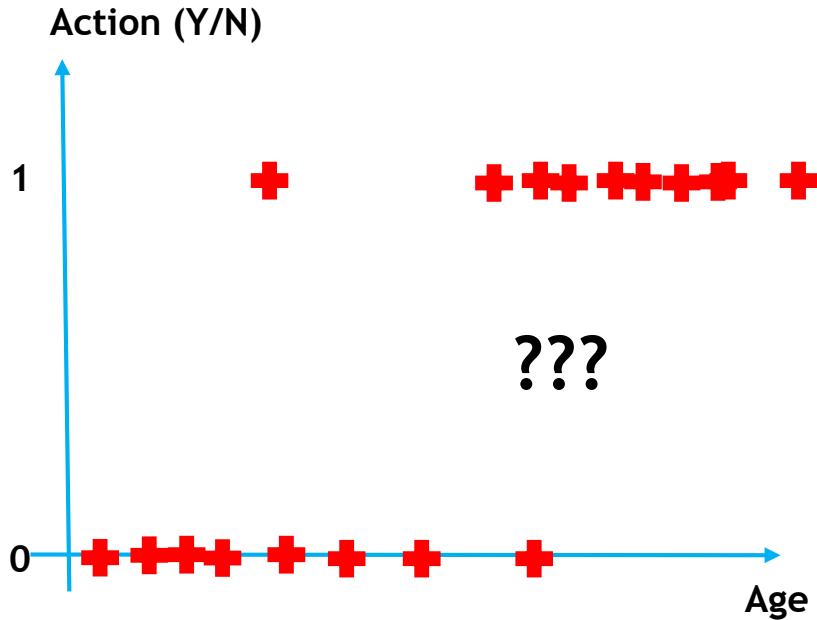




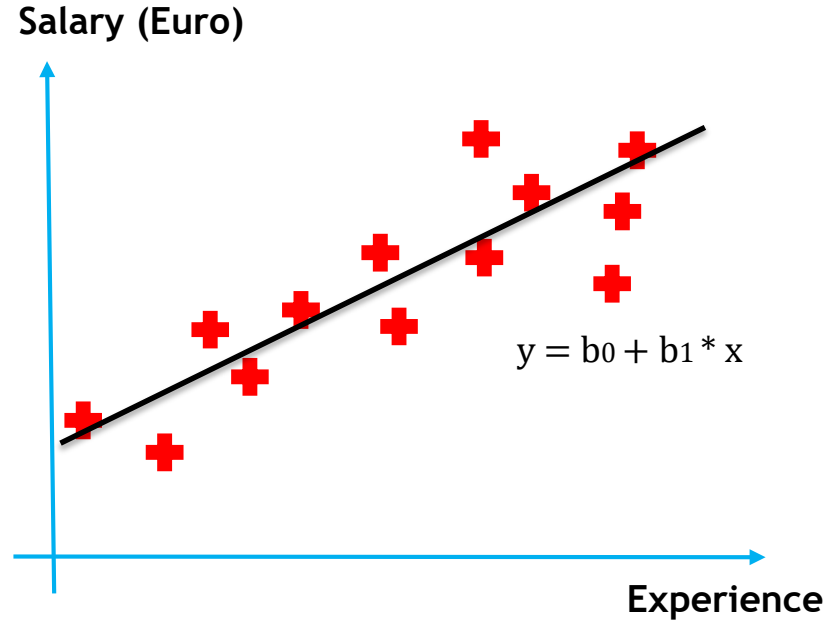


# Logistic Regression

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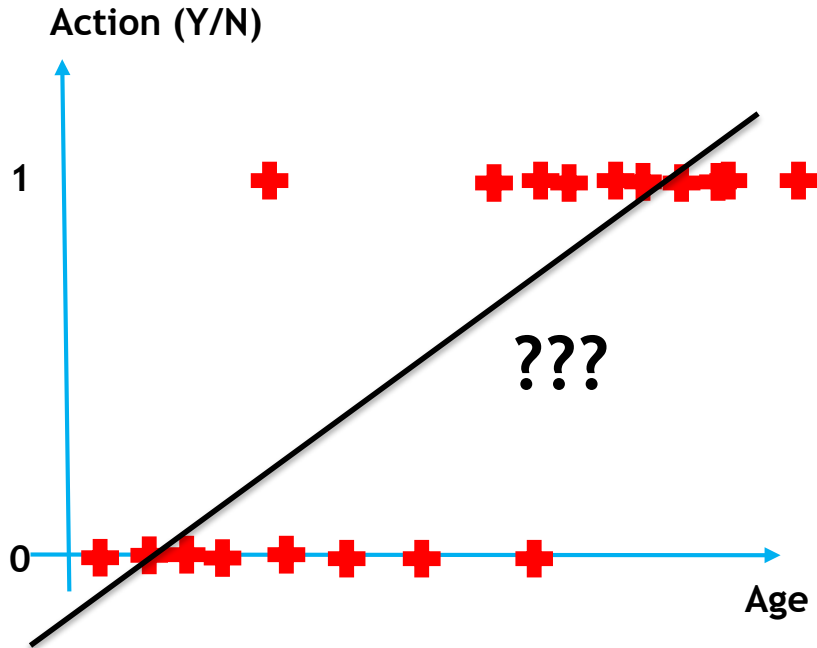
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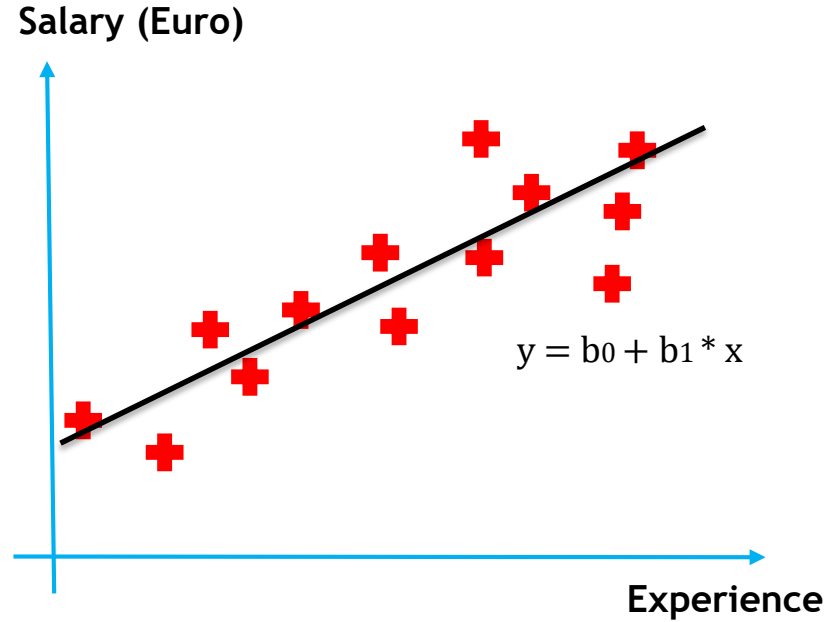


# Logistic Regression

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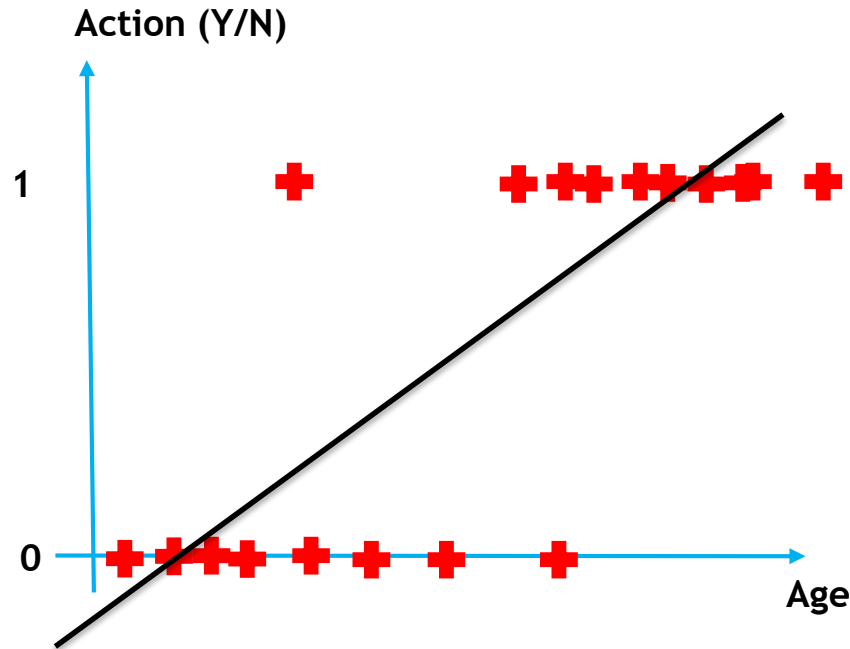


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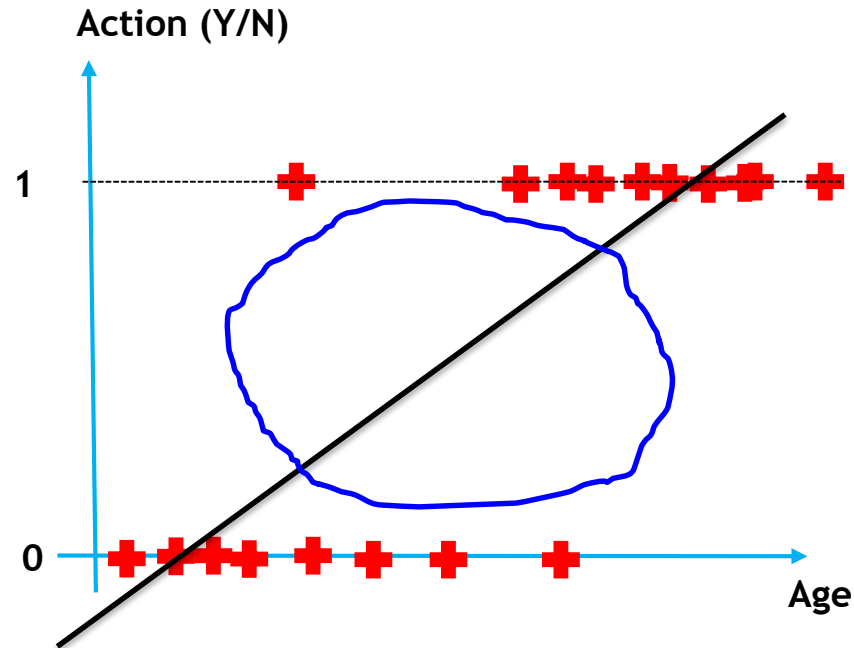


# Logistic Regression: what if predict the probability or likelihood a person taking the offer?



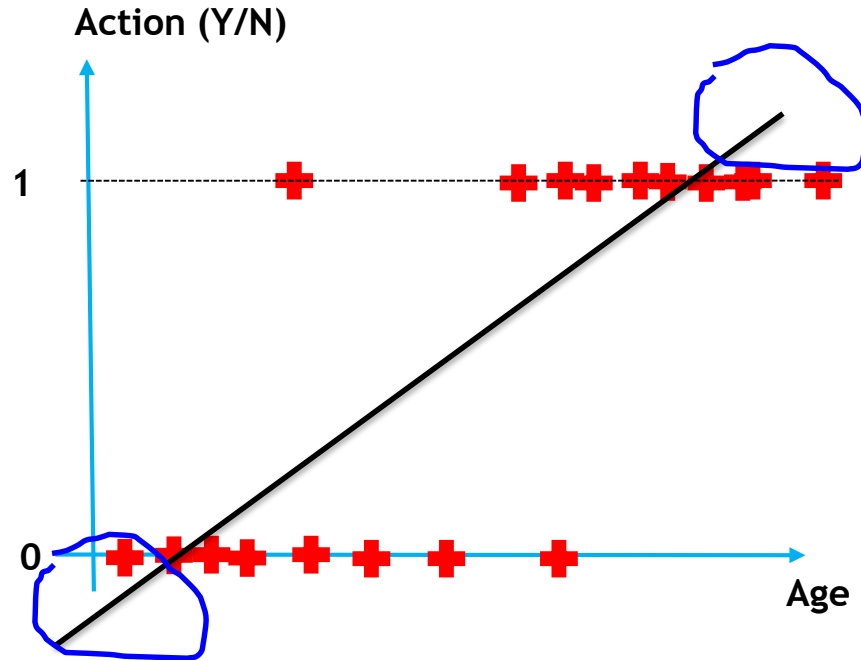


# Logistic Regression: this part make sense to get probabilities



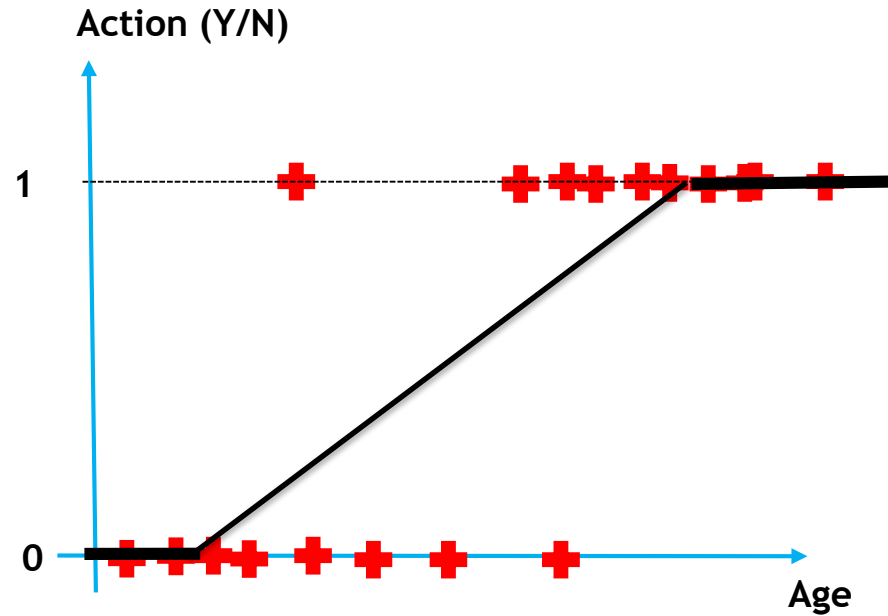


# Logistic Regression: this part does not make sense to get probabilities ( $<0>1$ )





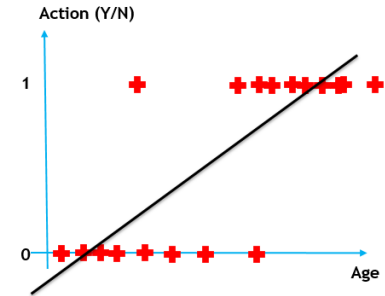
# Logistic Regression





# Logistic Regression

$$y = b_0 + b_1 * x$$



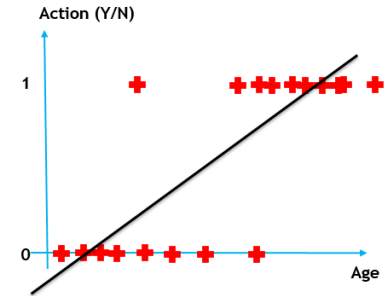
# Logistic Regression

$$y = b_0 + b_1 * x$$



Sigmoid Function

$$p = \frac{1}{1 + e^{-y}}$$





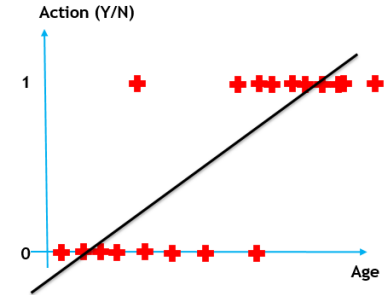
# Logistic Regression

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Sigmoid Function

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$$\ln\left(\frac{p}{1-p}\right) = b_0 + b_1 * x$$



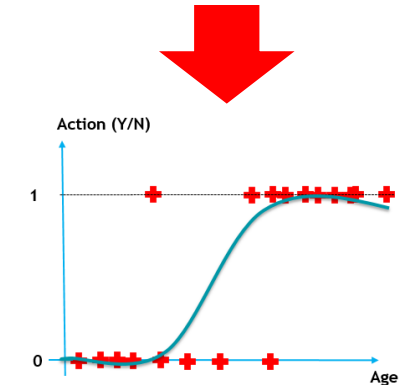
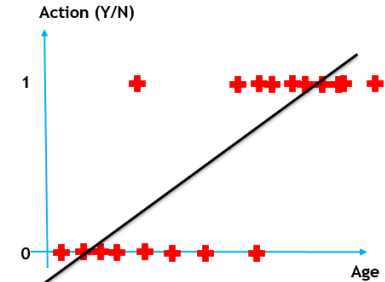
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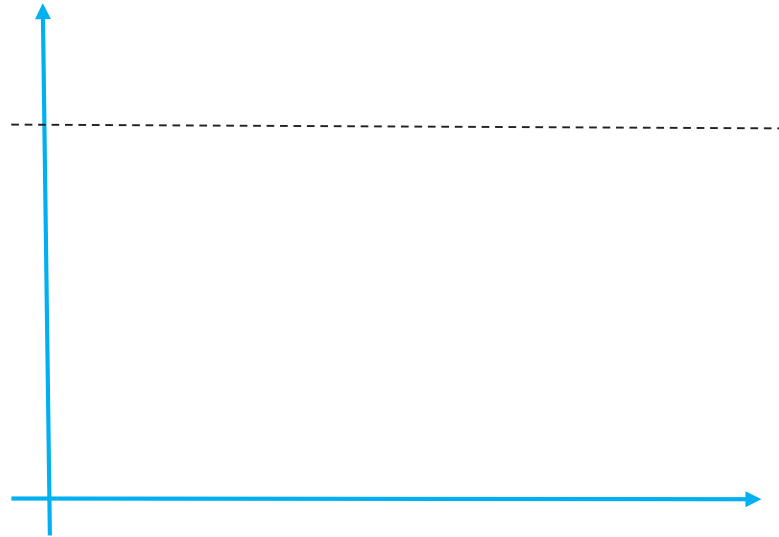
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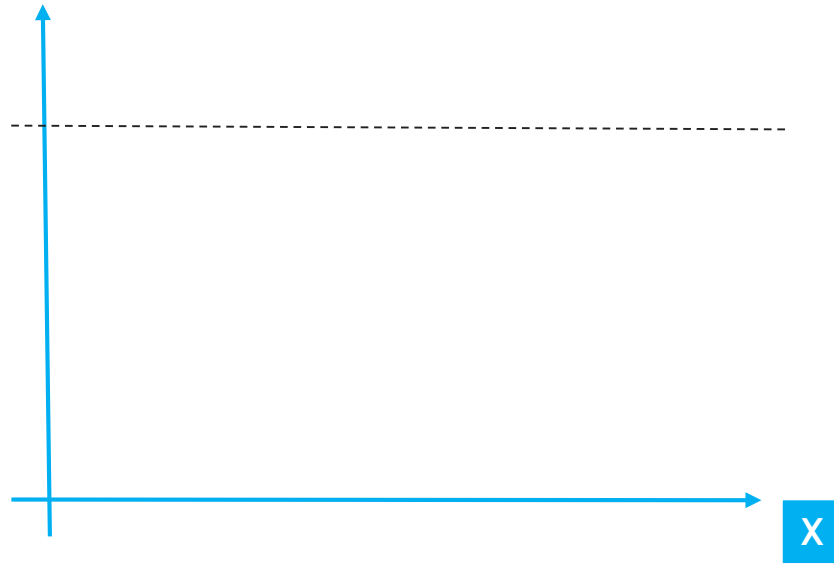




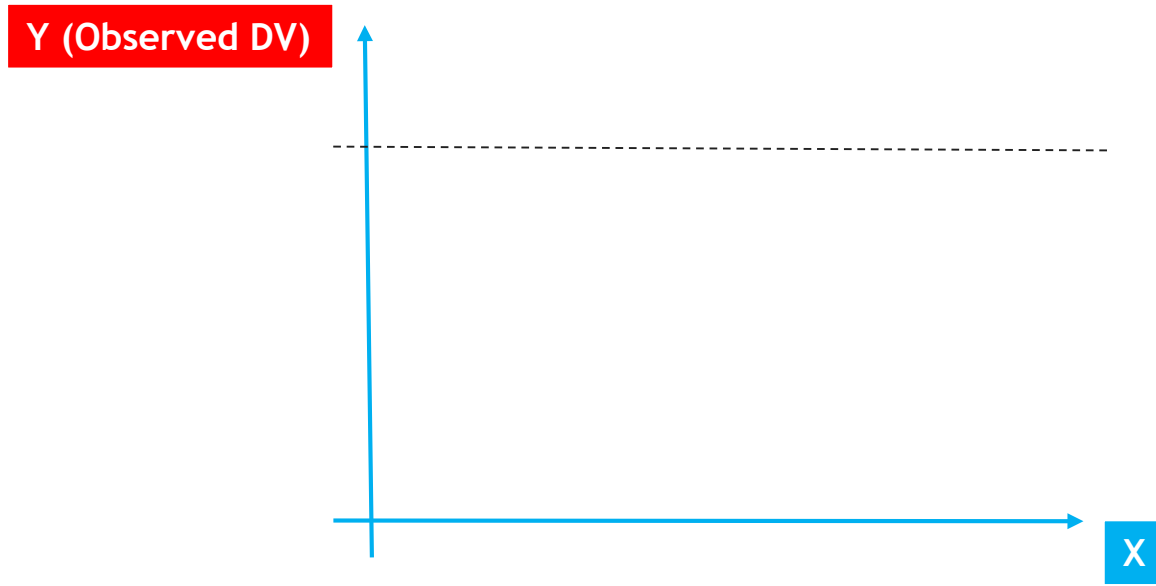
# Logistic Regression



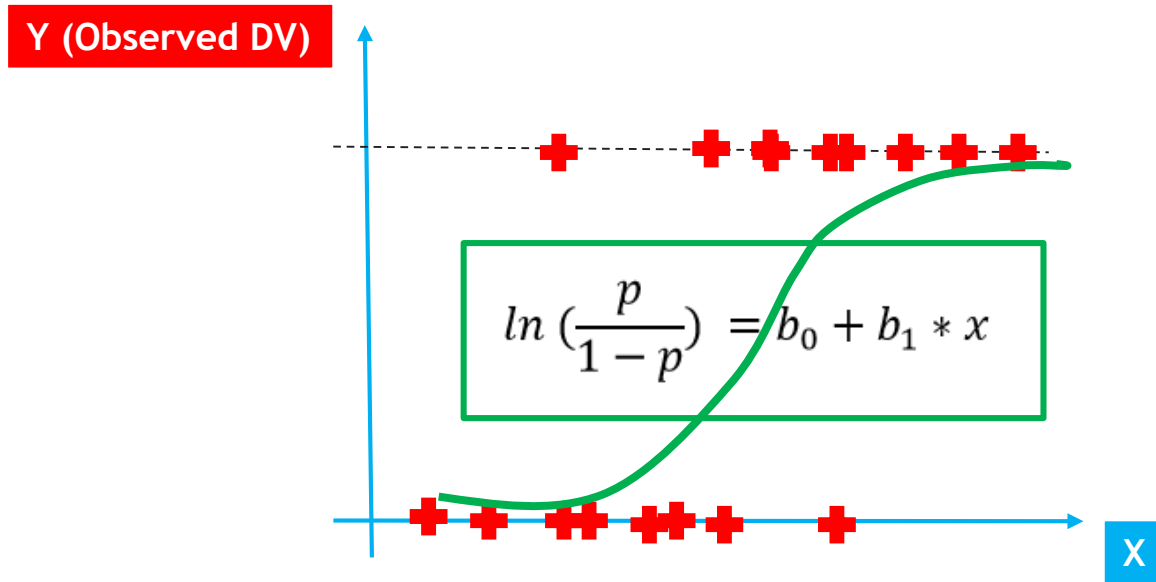
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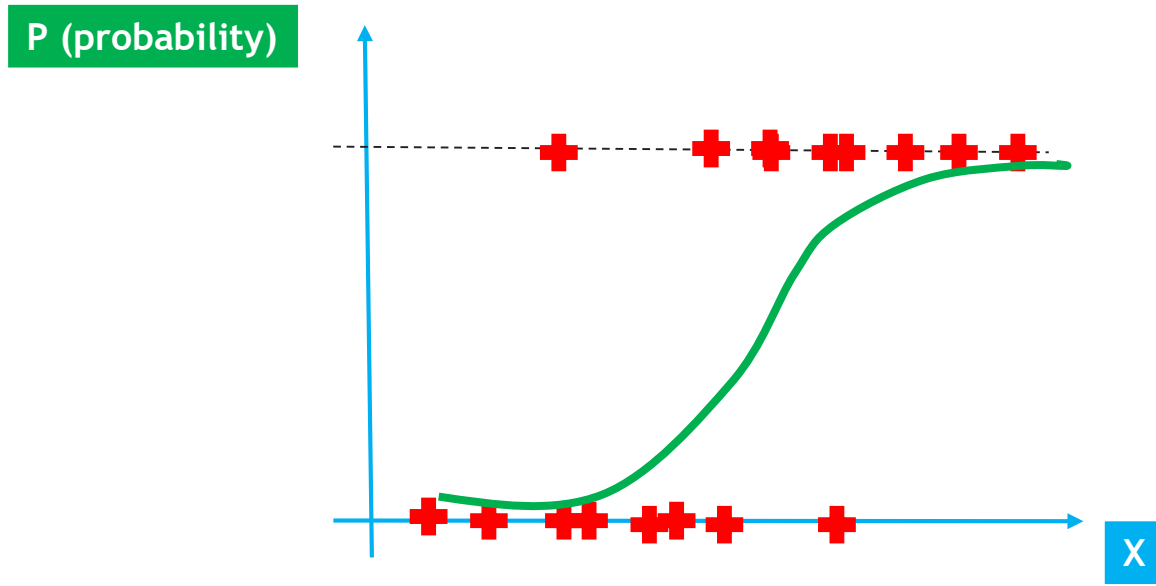
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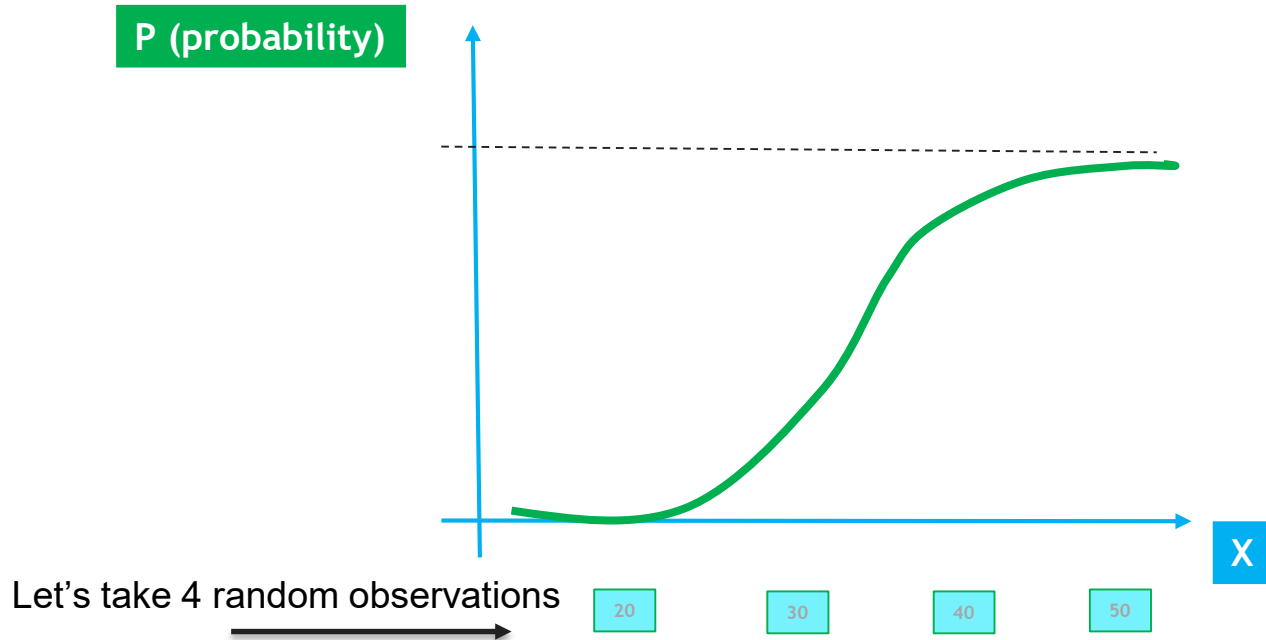
# Logistic Regression: best fitting line that fits our data



# Logistic Regression: we created the model

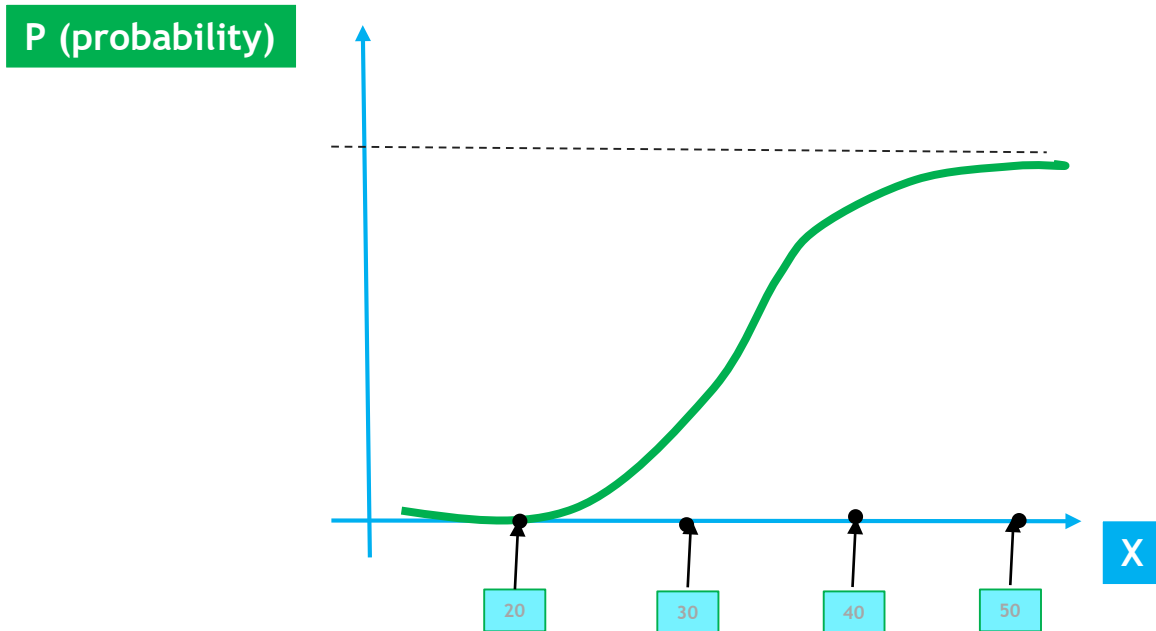


# Logistic Regression: we predict this probability



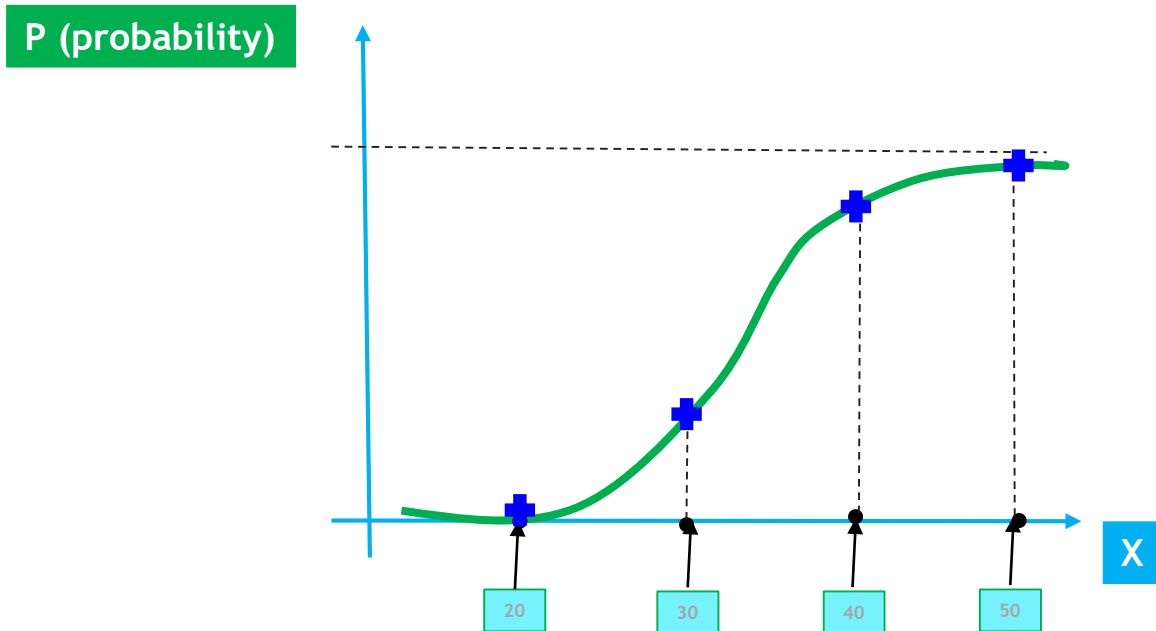


# Logistic Regression: what we need to do to get the probability of this 4 random variables?

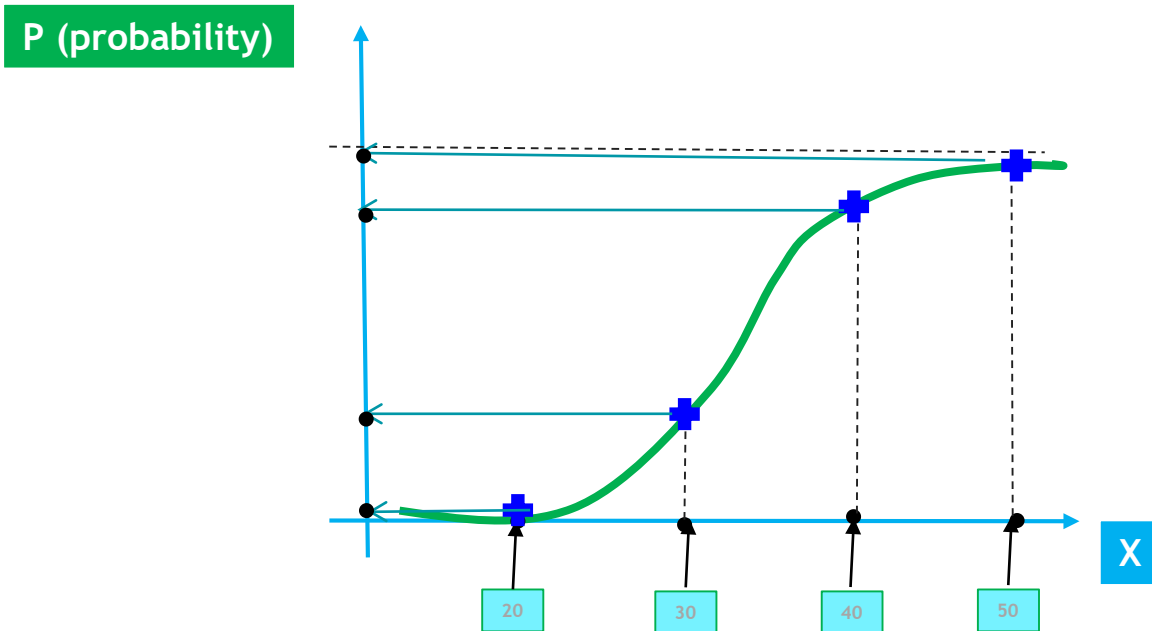




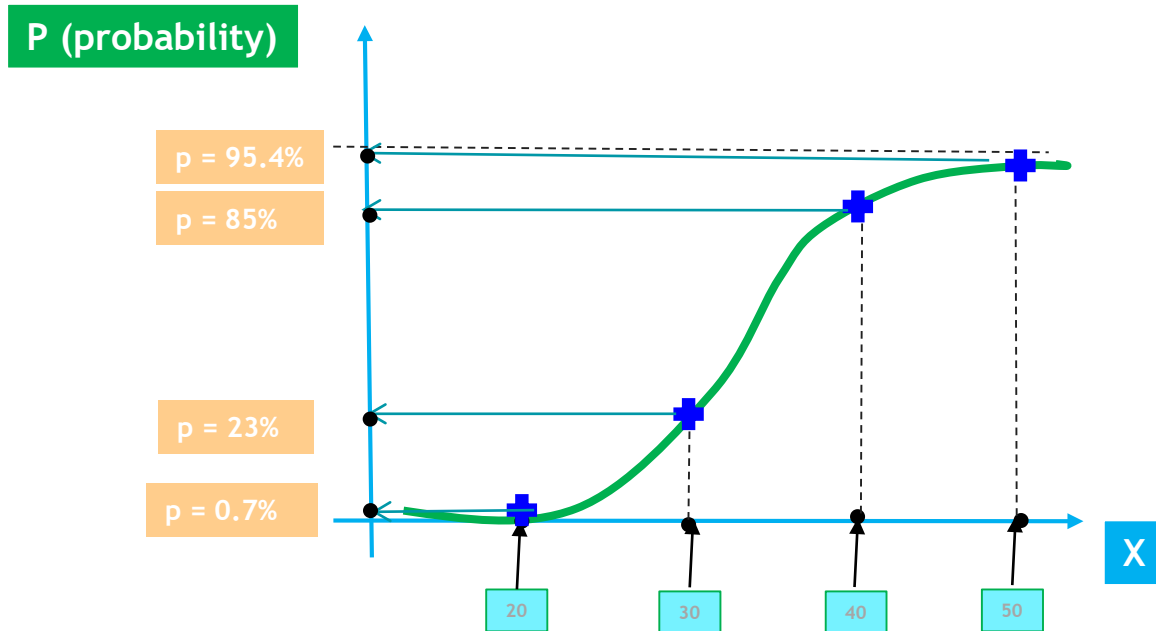
# Logistic Regression: we need to project them in the curve



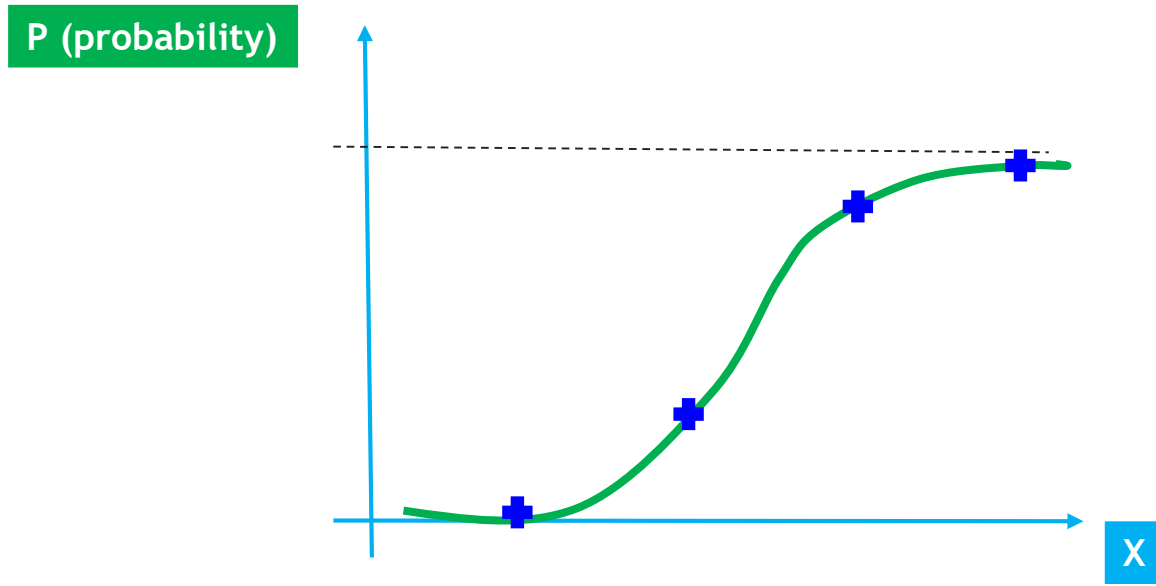
# Logistic Regression: if you need the probabilities, then it has to be projected to the left



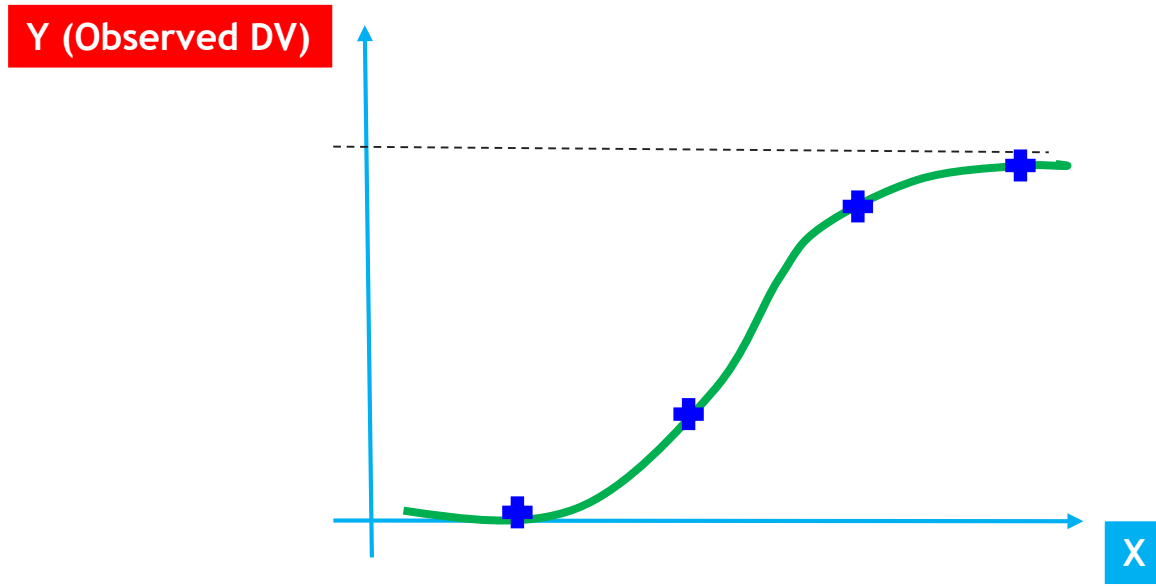
# Logistic Regression: who is the least/most likely to take the offer?



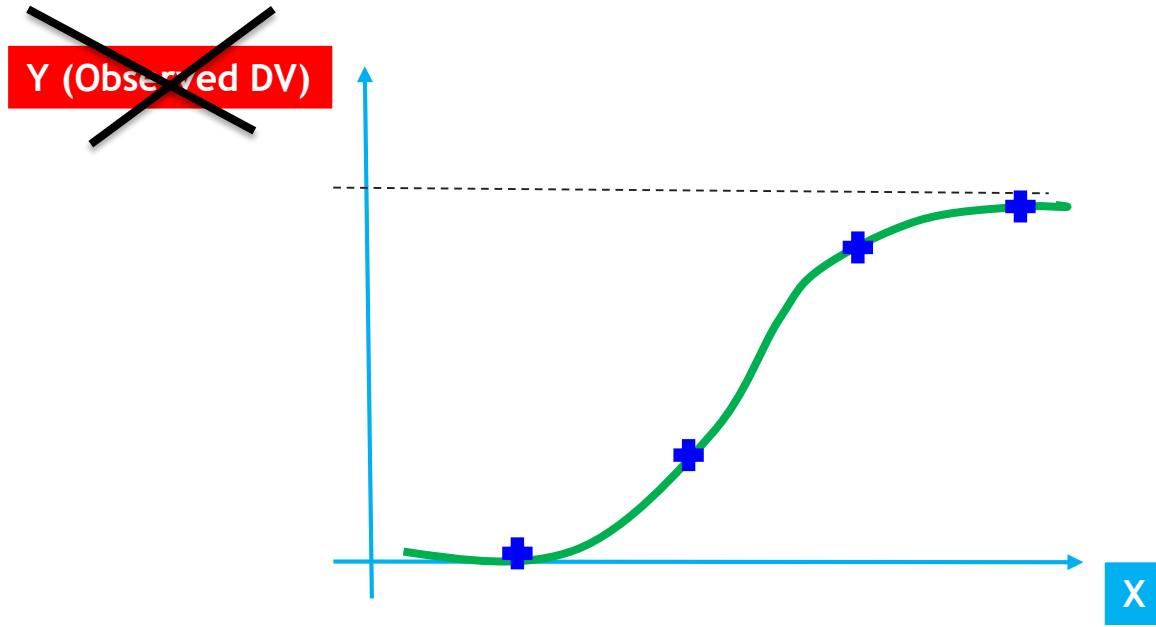
# Logistic Regression: I want a prediction instead probabilities



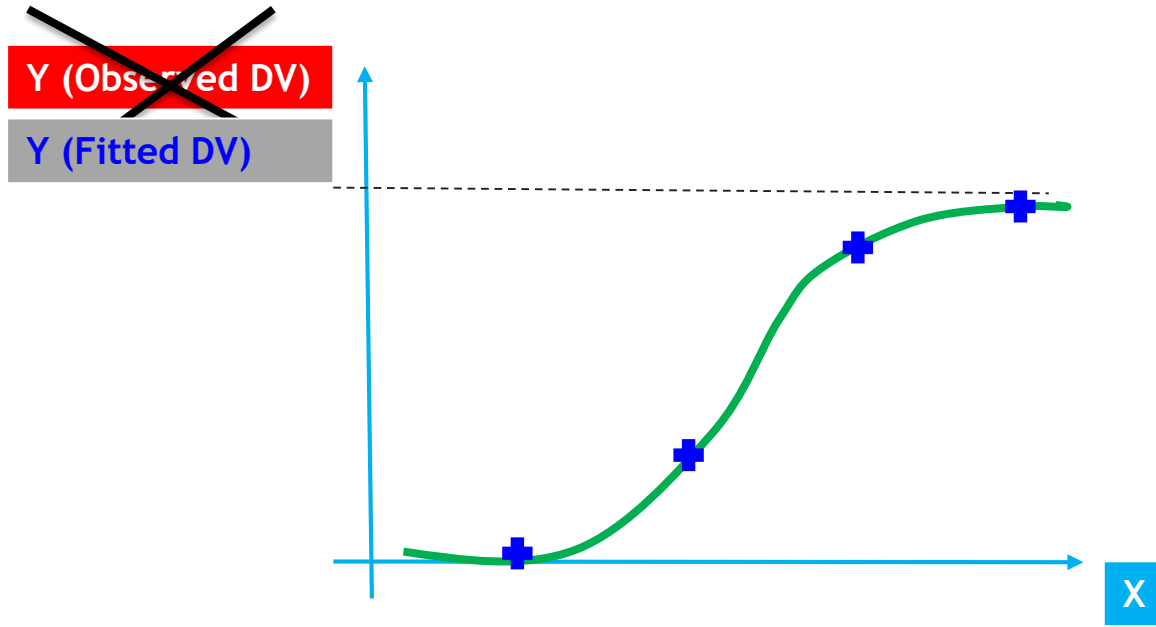
# Logistic Regression: get predicted (fitted) values



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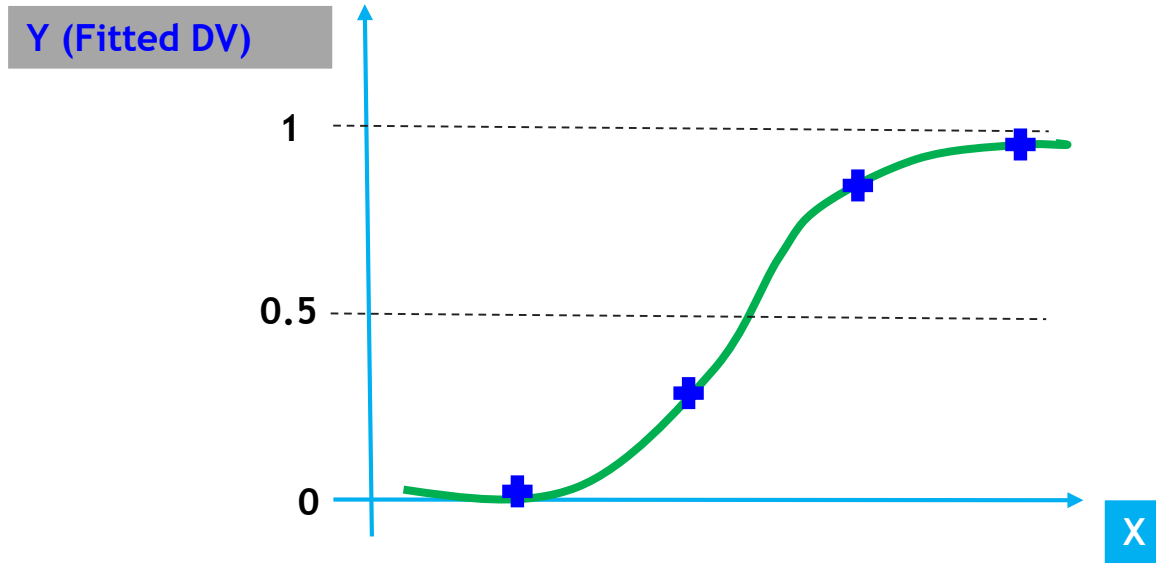


# Logistic Regression: get predicted (fitted) values

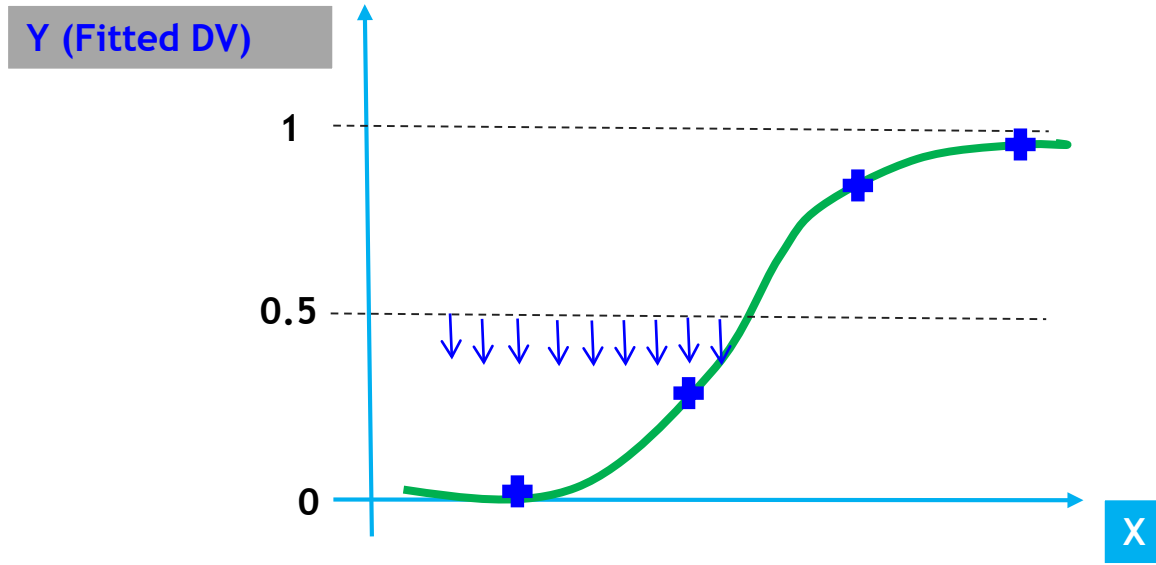




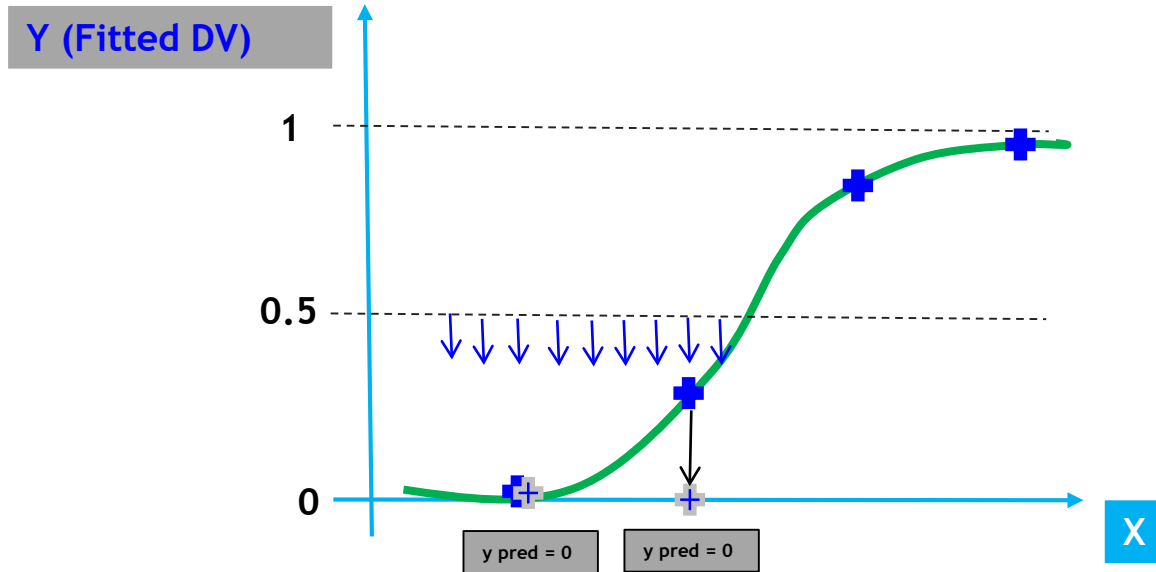
# Logistic Regression: select a threshold line



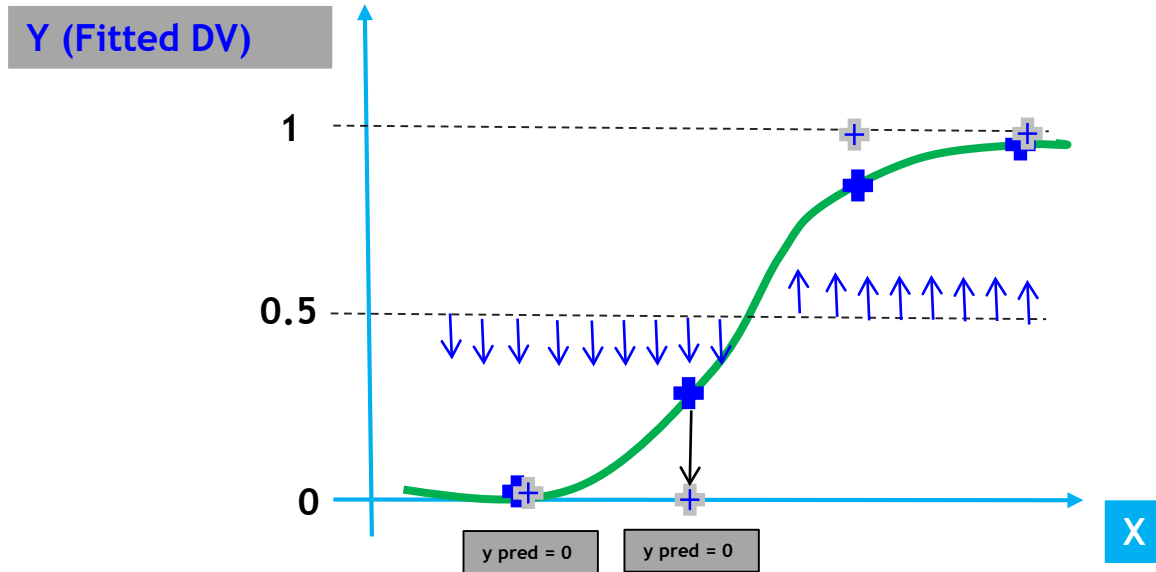
# Logistic Regression: if predicted probability is less than 50% then we predict 0



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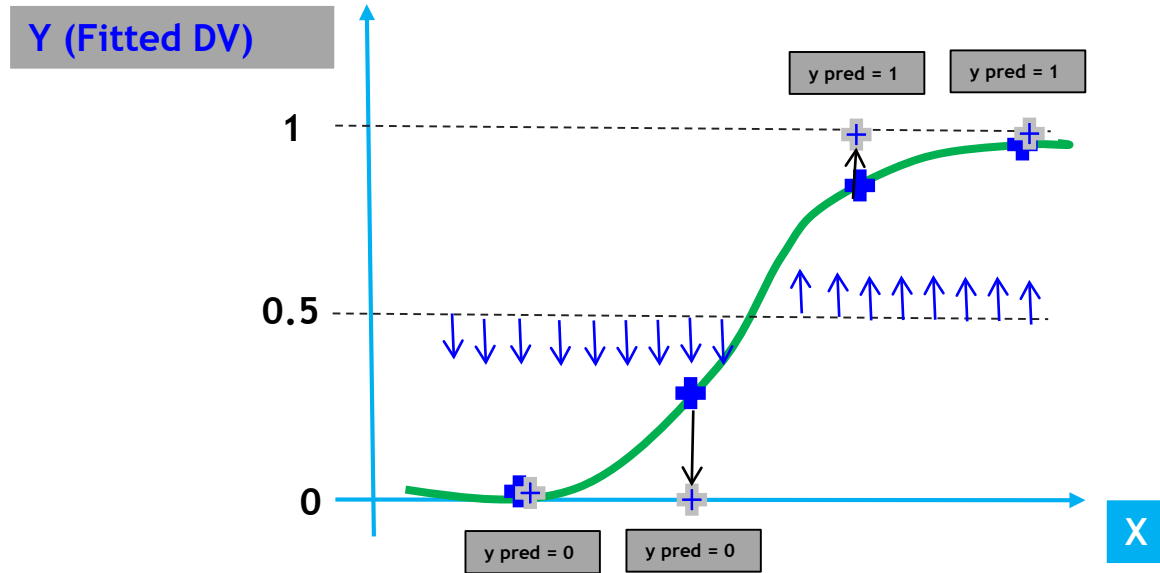


# Logistic Regression: anything above this threshold are predicted YES





# Logistic Regression: anything above this threshold are predicted YES





# Let's do it in R!!